



# SIGNIFICANT WAVE HEIGHT RETRIEVAL USING SENTINEL-1 SAR IMAGERY:

*Semi-empirical Investigation on Open Ocean Radar-look Directional Wave*

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## Research Objective

1. Evaluating semi-empirical update of significant wave height ( $H_s$ ) estimation applied to Sentinel-1 SAR repository for narrow-band swell-wave spectrum on the open-ocean waters **without prior knowledge or external inputs.**
2. Evaluate the dependency between  $H_s$  and local environment (wind forcing, wave type, SAR system limitation, and imaging mechanism)



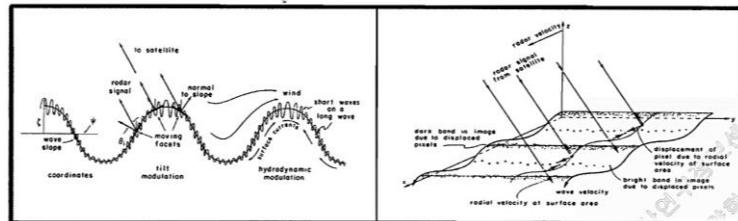
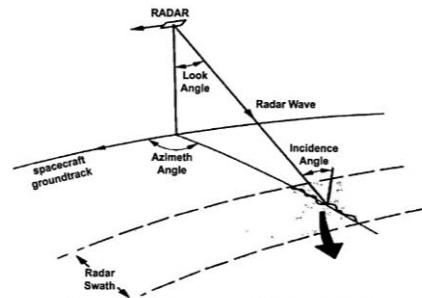
## New Approach of a Complimentary Work:

1. Updating the surface roughness and slope variation parameters derived from vertical polarization in a 5.405 GHz SAR system
2. Applying necessary digital filtering method for better peak of dominant wavelength identification in the frequency domain of 2D-Fast Fourier Transform
3. Evaluating the limitation and effects of varying wind speed and dominant wave type related to the nature of inear algorithm

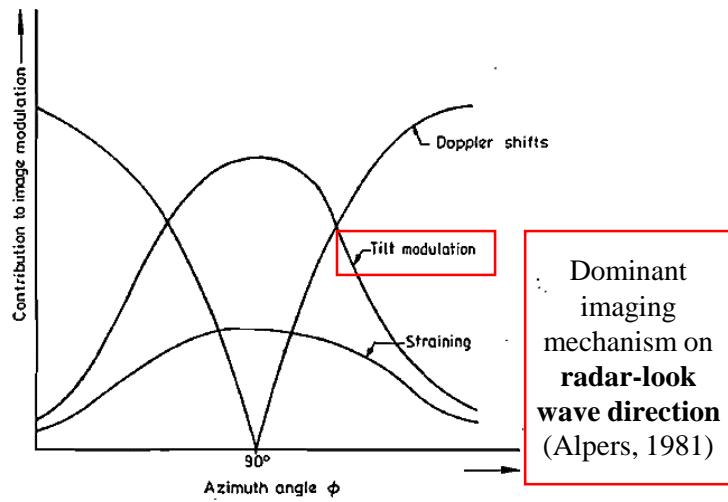
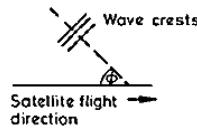


# SAR Capturing the Wave

1



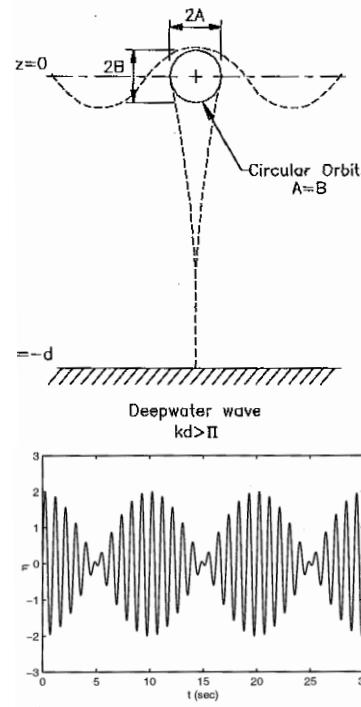
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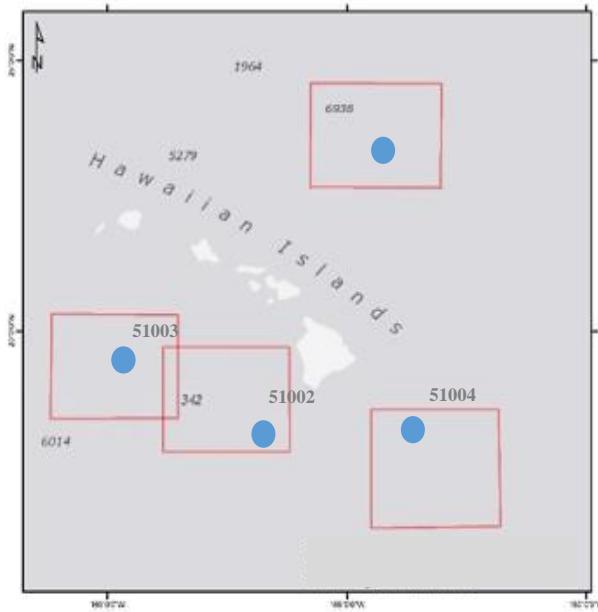
Radar system imaging ocean surface terminology (*upper left*), and Backscattered signal from moving ocean surface (*lower*). Dominated by Bragg scattering from capillary waves and short gravity waves, the composed waves in turn are modulated in their orientation, energy, and motion **by longer waves** on the bottom two images (Kim and Moon, 2003).

In the case of **swell**, the waves has strong space-time correlation and result in constructive velocity bunching. In **wind dominant sea**, however, the velocities are more random. The SAR processing usually becomes more destructive and apparent blurring (Swift and Wilson, 1979., Ardhuin, et al. 2015., Stopa, et al. 2015.)

3



# Area and Data

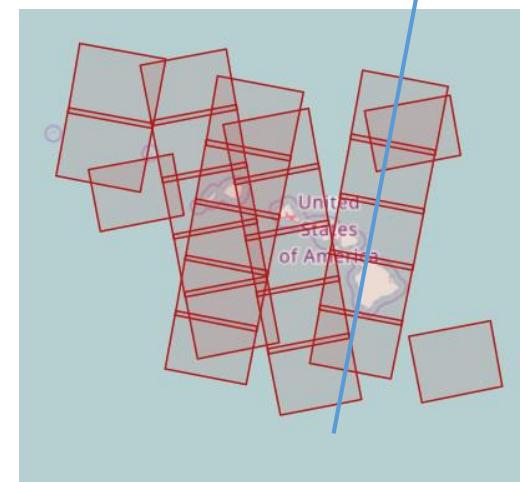


**Area of Interest :**  
Hawaii Waters  
(Oct 2016 – December 2017)

Offshore NDBC Buoys  
NDBC 51000, 51002,  
51004

Available Data : 143 scenes  
(69 scenes selected for  
radar-look directional wave)

Data Used are Ascending  
Sentinel 1A & 1B



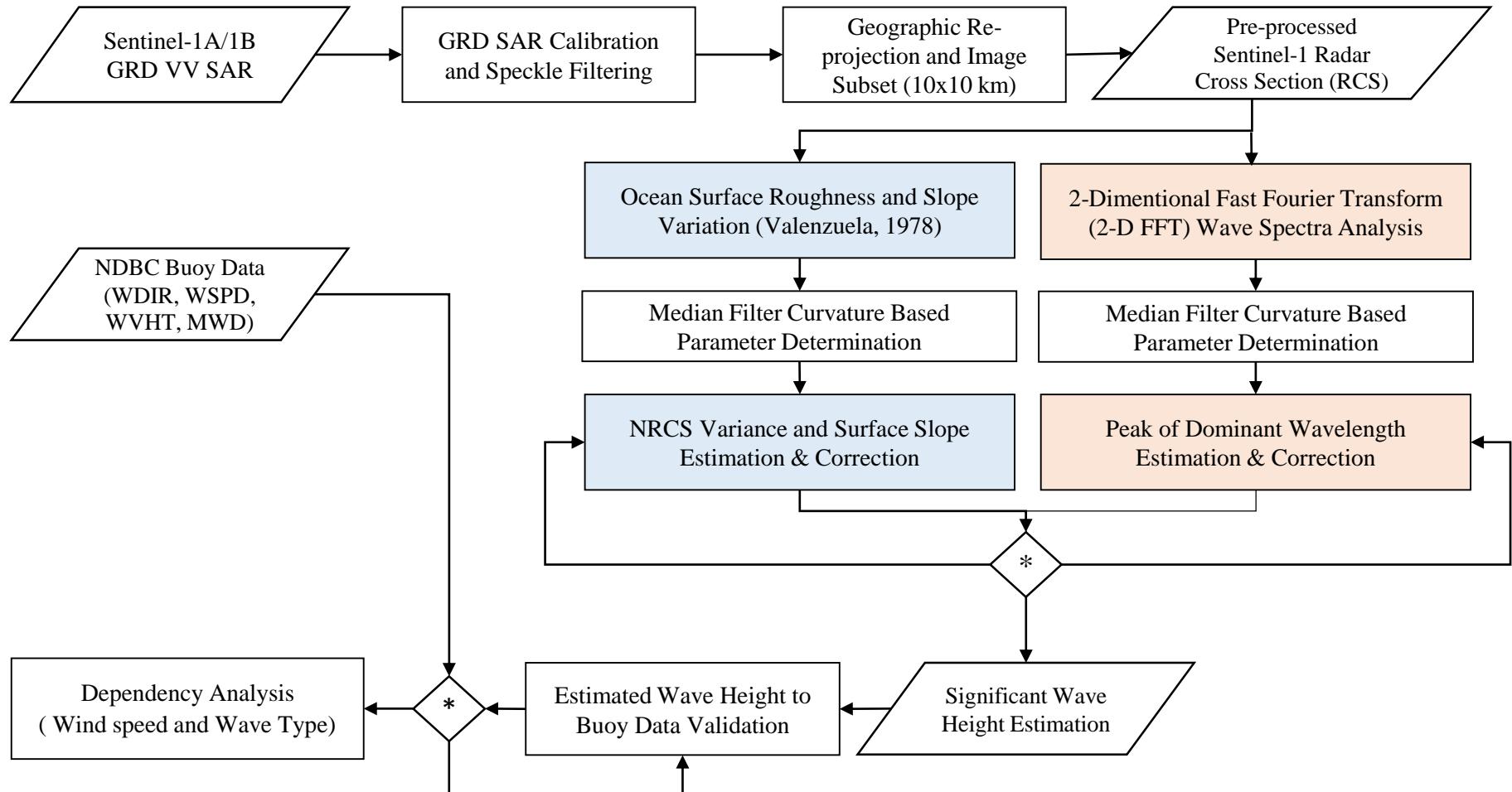
Data Example on NDBC Station 51004, HI

NDBC STATION 51004	DATE	TIME	#YY	MM	DD	hh	mm	WDIR	WSPD	GST	WVHT	DPD	APD	MWD	PRES	ATMP	WTMP	DEWP	VIS	TIDE	
			#yr	mo	dy	hr	mn	degT	m/s	m/s	m	sec	sec	deg	hPa	degC	degC	degC	nmi	ft	
S1A_IW_GRDH_1SDV_20161010T	10/10/2016	4:21:50	2016	10	10	3	50	42	7	8.1	2.01	14.8	6.62	351	1011.9	26.6	27	999	99	99	
				2016	10	10	4	50	45	7.8	9.1	1.93	14.8	6.57	333	1012.4	26.7	27	999	99	99
S1A_IW_GRDH_1SDV_20161022T	22/10/2016	4:21:50	2016	10	22	3	50	53	10.9	13.2	2.83	12.1	6.5	341	1012.7	27	26.8	999	99	99	
				2016	10	22	4	50	54	10.9	13.1	2.89	8.33	6.47	90	1013	26.9	26.8	999	99	99

Contents are taken from: <http://ndbc.noaa.gov/>



# Flowchart



(\*) Statistical assessment (outlier removal/ filtering/ linear regression)

Accuracy accepted or not



## Algorithm & Method

For a narrow-band swell-wave spectrum centered on wave number  $K_0$ , the r.m.s slope of the sea surface,  $\tan \Theta_r$ , is given (Thomas, 1982)

$$\frac{\tan \Theta_r}{H_s} = \frac{|K_0|}{4} = \frac{\pi}{2\lambda_0}$$

Using the equation above, if we know  $\tan \Theta_r$  and  $\lambda_0$ , it is **straight forward to determine  $\lambda_0$  by taking the 2 dimensional Fast Fourier Transform (2D-FFT) from a digital image**. On the other hand, the determination of  $\tan \Theta_r$  is based on the variation of the backscattering cross-section of the sea surface with incident angle (Valenzuela, 1978). Where  $\Theta$  is angle of the sea surface slope, and very small relative to the wavelength, we could rewrite those equation as follows:

$$\frac{\sqrt{\langle \theta^2 \rangle}}{H_s} = \frac{\pi}{2\lambda_0}$$

Below are several points need to be noted, to obtain the r.m.s. slope of the sea surface

1. Normalized Radar cross-section of sea surface changes with incidence angle [  $\sigma_0 = \sigma_0(\Theta)$  ]
2. where  $\Theta$  represents the SAR wave incidence angle, the NRCS ( $\sigma_0$ ) will change within the various  $\Theta$
3. Because of the tilt modulation, there is a small incidence angle change due to the sea surface slope relative to the mean surface. This, if the sea surface slope angle is  $\Theta$ , the incidence angle for the tilted sea surface is [  $\Theta = \Theta_0 - \theta$  ]

$$\sqrt{\langle \theta^2 \rangle} = \sqrt{\langle [\sigma_0(\Theta_0 - \theta) - \sigma(\Theta_0)]^2 \rangle} / \left. \frac{d\sigma_0}{d\theta} \right|_{\Theta=\Theta_0}$$

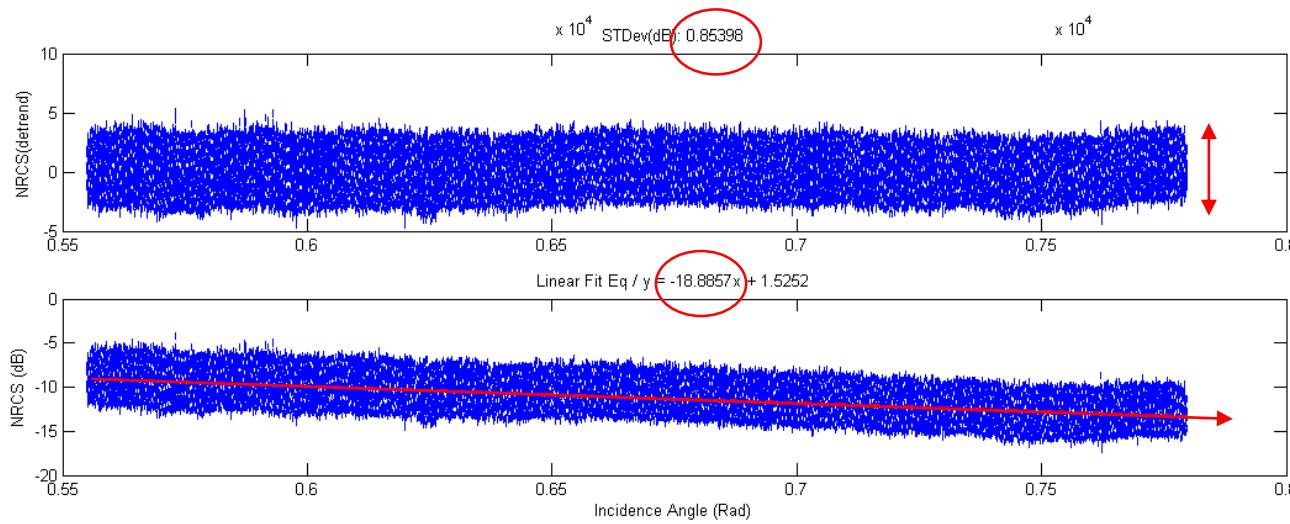
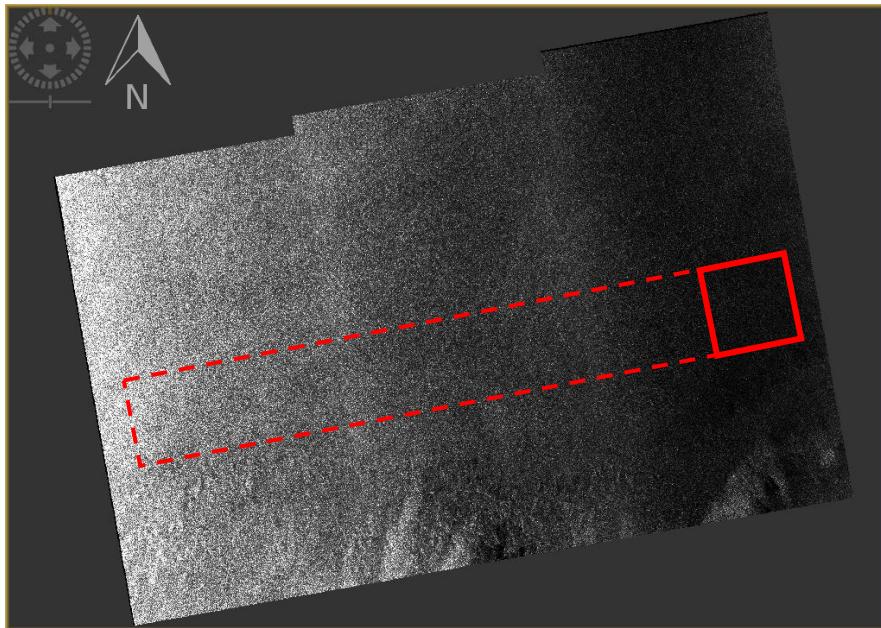
where  $\sqrt{\langle [\sigma_0(\Theta_0 - \theta) - \sigma(\Theta_0)]^2 \rangle}$  is the standard deviation of  $\sigma_0$ , denoted as  $\text{std}(\sigma_0)$ . Therefore, we have equation below explaining the r.m.s slope of the sea surface as seen in the original equation

$$\sqrt{\langle \theta^2 \rangle} = \text{std}(\sigma_0) / \left. \frac{d\sigma_0}{d\theta} \right|_{\Theta=\Theta_0}$$

These parameters gives us the simple empirical-physical properties of swell-waves happens, assuming that the wavelength are constant and linearly distributed over a subset of image. Thus, this equation is not suitable for understanding phenomena such as internal waves and very low to extreme sea state condition. Those boundaries of application will be explained later.

# Result

## Ocean Surface Roughness and Slope Variation (Valenzuela, 1978)

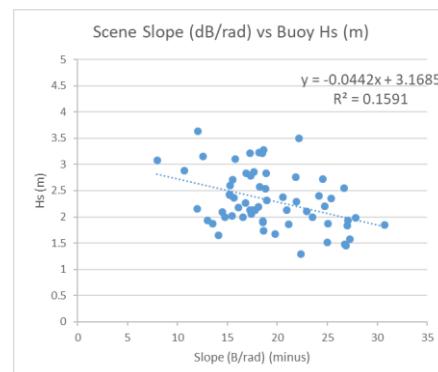
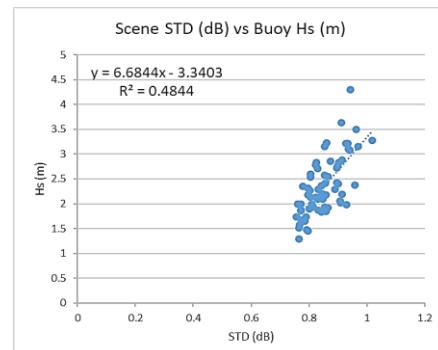


Two subset are taken from each scene:

1. 1000 pixels rectangular subset for empirical standard deviation
2. 1000 pixels width for the entire length of the image for consistent ocean surface slope

Result from 69 scenes plot below :

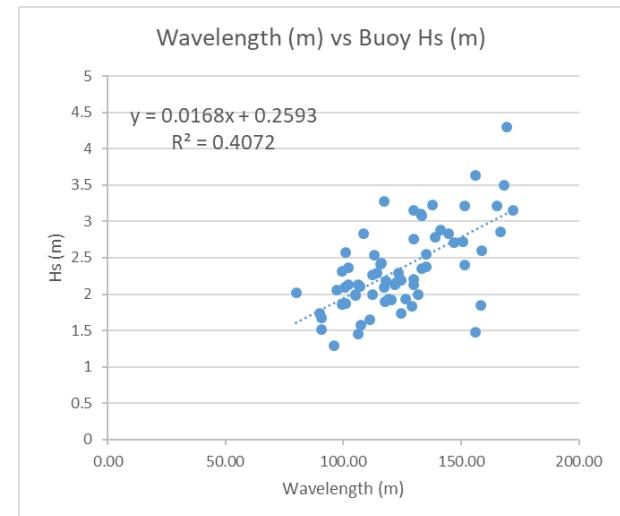
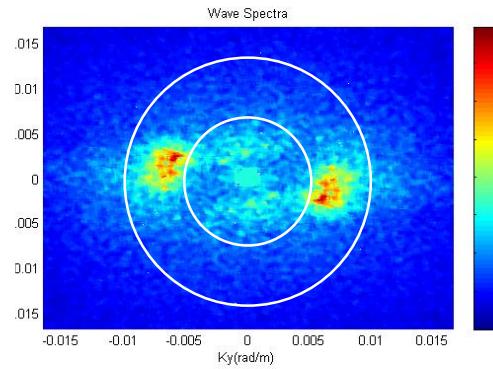
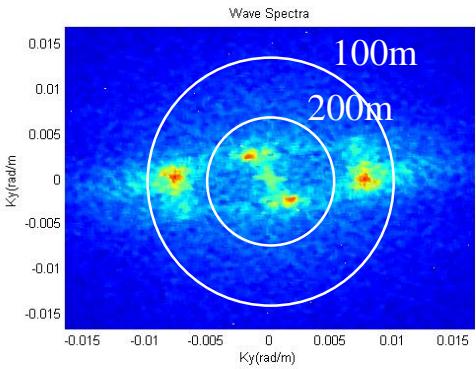
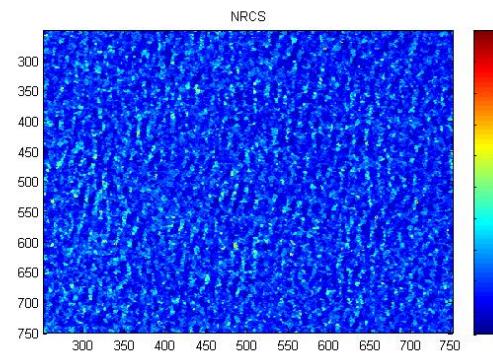
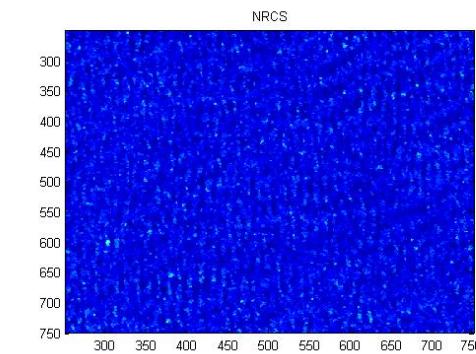
1. The standard deviation (dB) grows stronger with  $\gg H_s$
2. The slope (dB/ radians) is relatively steeper with  $\gg H_s$



# Result

## 2-Dimentional Fast Fourier Transform (2-D FFT) Wave Spectra Analysis

5x5 pixels parameterized median filter is applied to the radar cross section based on it's effectivity to enhanced the dominant wavelength peak, while 2D Gaussian filter is applied on the frequency domain to reduces the low frequency noise in the middle of the wave spectra.



Result from 69 scenes plot below :  
The wavelength (m) grows stronger with higher Hs.

Some of the result fails this common pattern due to the high wind speed ( $> 10 \text{ ms}^{-1}$ ) or wind wave dominant sea.

# Estimated Hs Result

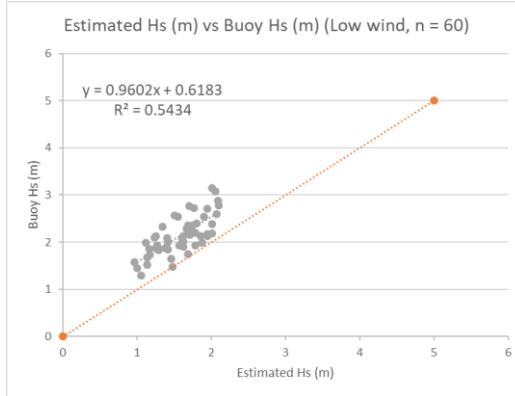
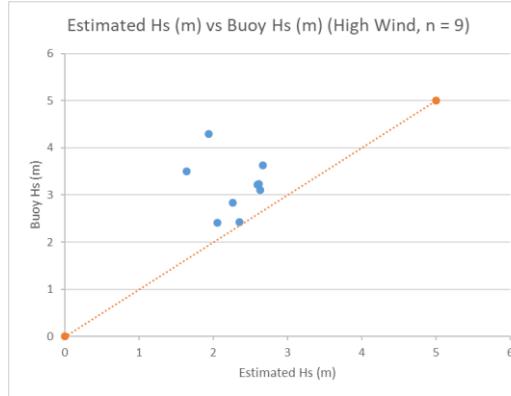
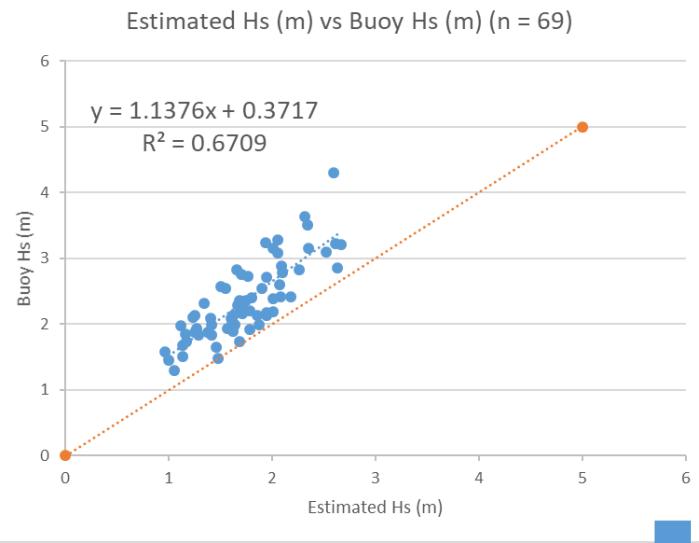


Figure above shows the different between high 10m above sea level wind ( $>10\text{ms}^{-1}$ ) condition (left) with low to medium wind speed (right) before the linear regression applied

We found 0.3717m overestimation compared to the buoy data and applied the linear regression

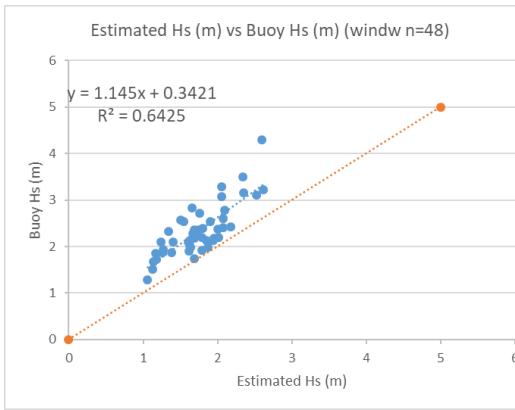
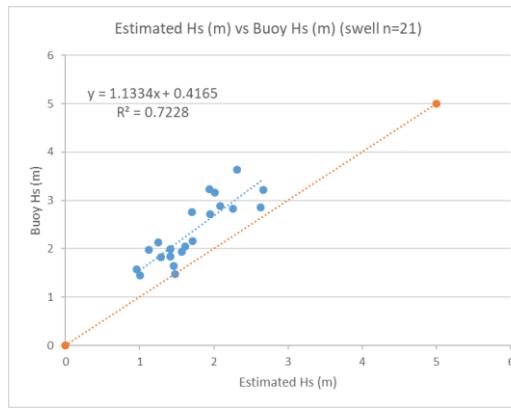
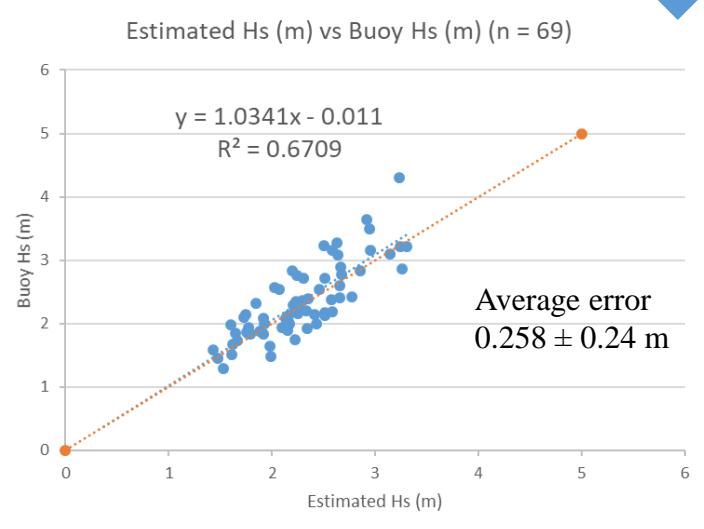
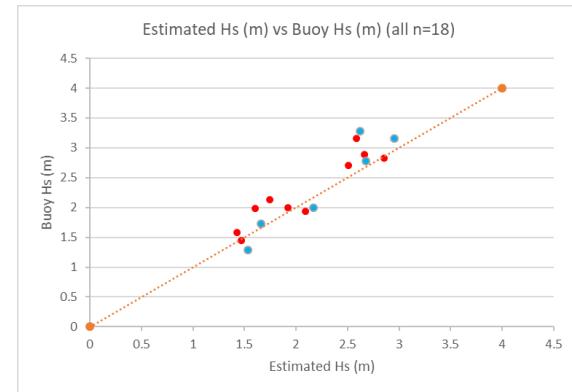
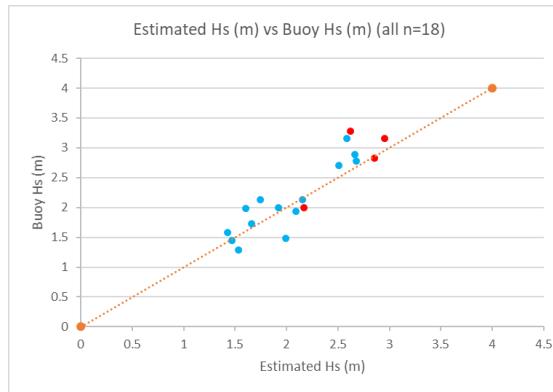
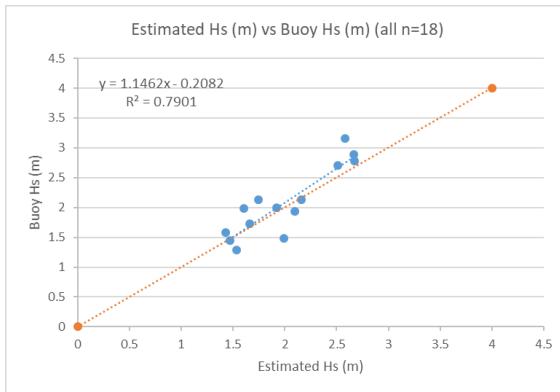


Figure above shows the different between swell dominant sea (left), and wind dominant sea (right) before the linear regression applied

# Estimated Hs Result NBDC51000

51000 BUOY	STD	SLOPE		WVDIR	WLNGTH	Hs	Corr. Hs		WDIR	WSPD	BUOY HS	MWD		$\Delta$ Hs
20161022T042324	0.82564	16.86361		87.51045	144.92754	2.258609	2.85446949		69	10.25	2.83	196.5		0.024469
20161127T042324	0.85307	12.54231		92.96094	172.41379	2.349041	2.95394481		85.5	11.45	3.155	95.5		0.201055
20161221T042323	0.914858	10.70636		98.93059	142.85714	2.086743	2.6654168		86.5	8.2	2.885	336		0.219583
20170303T042320	1.017392	18.58472		93.36646	117.64706	2.050044	2.6250486		110	12.4	3.28	88.5		0.654951
20170514T042323	0.8224	17.35266		91.59114	138.88889	2.095244	2.67476837		97.5	5.9	2.78	121.5		0.105232
20170713T042326	0.766734	27.2433		88.76802	107.52688	0.963279	1.42960658		53.5	5.05	1.58	355		0.150393
20170725T042327	0.930302	27.80714		87.58897	105.26316	1.120971	1.60306778		95.5	6.35	1.98	146		0.376932
20171005T042330	0.806426	20.94887		92.33731	102.04082	1.250339	1.74537295		66.5	6.55	2.135	124		0.389627
20171017T042330	0.82886	15.52268		90.84252	147.05882	1.946192	2.51081134		90	3.8	2.71	315.5		0.199189
20171216T042329	0.970432	35.61468		92.97373	129.87013	2.012276	2.58350401		20	3.6	3.155	319.5		0.571496
20170426T042240	0.814942	13.01557		98.22672	120.48193	1.567695	2.09446451		75.5	6.3	1.935	184.5		0.159465
20170520T042241	0.796409	26.8995		89.39049	106.38298	1.002569	1.4728262		107	7.35	1.45	37.5		0.022826
20170601T042242	0.761406	23.51906		73.951	136.9863	1.411639	1.92280276		80.5	8.2	1.995	308		0.072197
20170613T042243	0.809963	16.56542		88.19126	105.26316	1.638285	2.17211305		84.5	10.2	1.99	63		0.182113
20170707T042244	0.765188	22.37789		82.25966	97.087379	1.056724	1.53239669		71	5.1	1.29	69.5		0.242397
20170719T042245	0.757085	32.67595		67.81599	97.087379	1.173601	1.6609616		86.5	5.5	1.73	48.5		0.069038
20170731T042245	0.791729	26.70793		86.42367	156.25	1.474371	1.99180764		55	5.65	1.48	132		0.511808
20170824T042247	0.826893	17.23459		88.17203	106.38298	1.624691	2.15715999		80	8.65	2.125	76.5		0.03216
													MAX	0.654951
													STD	0.192493
													MEAN	0.232496



All Data

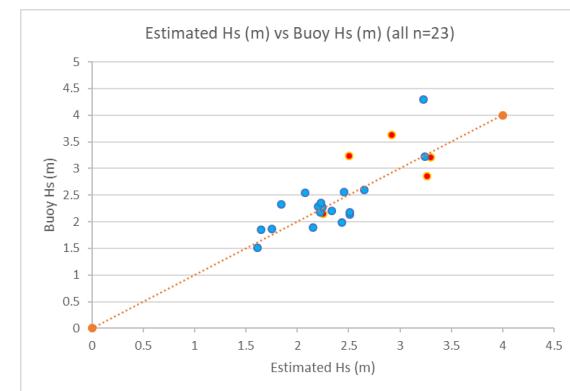
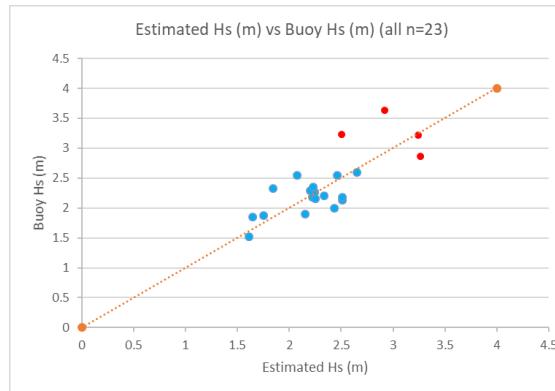
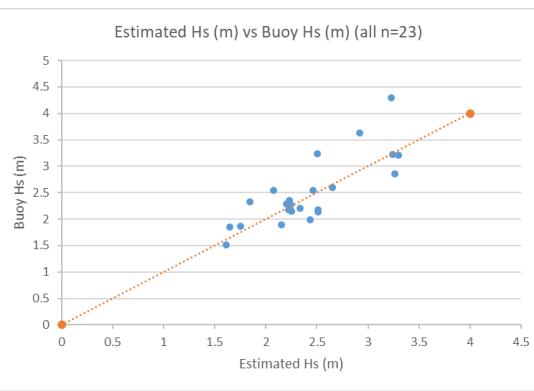
Red : High Wind  
Blue: Low- Med Wind

Red : Swell  
Blue: Wind Wave

# Estimated Hs Result NBDC51004

51004 BUOY	STD	SLOPE		WVDIR	WLNGTH	Hs	Corr. Hs		WDIR	WSPD	BUOY HS	MWD		$\Delta$ Hs
20161022T042140_	0.874279	17.63204		91.90915	166.66667	2.630549	3.26360425		53.5	10.9	2.86	215.5		0.403604
20161103T042140_	0.865824	26.6801		90.77422	135.13514	1.90089	2.46097924		61	8.2	2.545	84		0.084021
20161115T042140_	0.860342	18.16416		97.12502	138.88889	1.941323	2.50545486		68.5	10.9	3.23	300.5		0.724545
20161127T042140_	0.911781	12.02273		90.89517	156.25	2.314567	2.91602372		69	12.05	3.635	202		0.718976
20161221T042139_	0.935029	17.27665		92.60256	151.51515	2.610188	3.24120675		56.5	10.25	3.22	92.5		0.021207
20170102T042137_	0.859727	30.92877		101.5752	120.48193	1.682834	2.22111783		24	3.9	2.18	41		0.041118
20170114T042137_	0.852763	11.95477		97.7336	123.45679	1.710419	2.25146141		86	9	2.155	219.5		0.096461
20170303T042136_	0.824191	17.52745		90.07441	129.87013	1.943875	2.50826296		106	6.25	2.13	77		0.378263
20170327T042137_	0.927765	18.466		97.59464	166.66667	2.665409	3.3019504		77	10	3.215	198		0.08695
20170514T042139_	0.803137	16.84089		91.28733	112.35955	1.705629	2.24619159		72.5	8.65	2.27	49.5		0.023808
20170725T042143_	0.772183	14.72319		91.28733	112.35955	1.875766	2.43334268		72.5	8.4	1.99	77.5		0.443343
20170806T042144_	0.831062	21.88593		92.82712	123.45679	1.666892	2.2035817		61.5	9.55	2.285	87.5		0.081418
20170911T042145_	0.772803	25.08942		94.00417	100	1.255533	1.75108595		64	6.9	1.87	101		0.118914
20170426T042056_	0.84585	24.70967		90.74406	129.87013	1.784686	2.33315444		79	7.95	2.2	97.5		0.133154
20170508T042056_	0.797363	16.08628		87.17288	123.45679	1.947896	2.5126858		101.5	8.35	2.175	57		0.337686
20170520T042057_	0.800546	18.52198		89.32596	117.64706	1.618566	2.15042231		64.5	7.45	1.895	85.5		0.255422
20170601T042058_	0.805121	15.24979		88.1817	158.73016	2.076251	2.65387633		66	9.75	2.6	107.5		0.053876
20170719T042101_	0.765665	24.98263		90.52086	90.909091	1.13085	1.61393496		78	6.25	1.515	118		0.098935
20170812T042102_	0.771141	21.10514		95.14276	100	1.163042	1.64934631		64	8.35	1.855	82		0.205654
20170824T042102_	0.796415	18.94568		95.14276	100	1.338071	1.84187827		60.5	9.05	2.32	92.5		0.478122
20171023T042104_	0.805779	18.83365		95.19443	113.63636	1.547565	2.07232189		82	7.15	2.54	101.5		0.467678
20171116T042104_	0.779714	25.38383		90.7639	133.33333	1.689015	2.22791613		46	8.7	2.355	30.5		0.127084
20171128T042104_	0.944	17.29433		90.97102	169.49153	2.599436	3.22937918		69	11.25	4.3	18	1.070621	0.280472

NDBC 51004



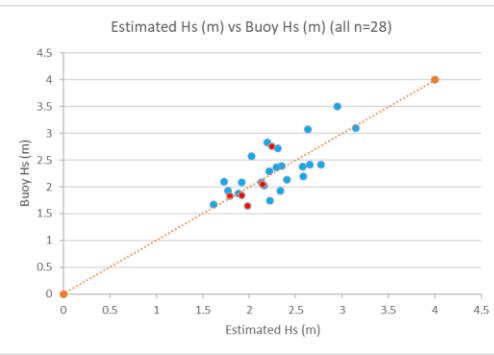
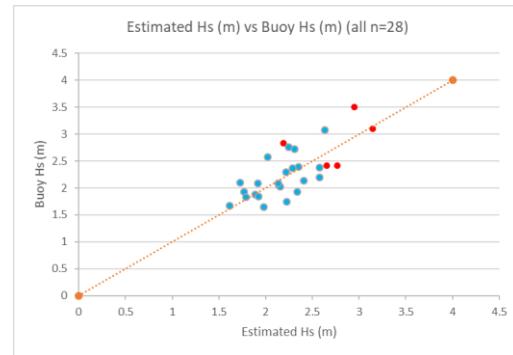
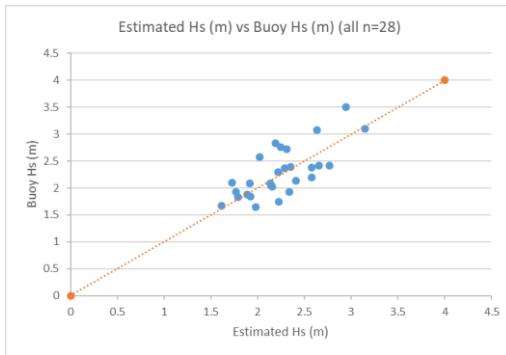
All Data

Red : High Wind  
Blue: Low- Med Wind

Red : Swell  
Blue: Wind Wave

# Estimated Hs Result NBDC51002

51002 BUOY	STD	SLOPE		WVDIR	WLGTH	Hs	Corr. Hs		WDIR	WSPD	BUOY HS	MWD		$\Delta$ Hs
20161101T043802	0.93716	15.76064		95.33216	133.33333	2.523646	3.14601088		63.5	10.9	3.1	76		0.046011
20161207T043801	0.957645	20.53878		91.54816	135.13514	2.005619	2.57618106		62	4.25	2.38	73		0.196181
20161231T043800	0.90657	17.39849		90.55625	97.087379	1.610286	2.14131414		55.5	6.7	2.05	353		0.091314
20170124T043758	0.962109	22.16477		96.76617	169.49153	2.341849	2.94603405		61	9.95	3.5	83		0.553966
20170301T043758	0.848465	40.2201		85.95551	101.0101	1.406476	1.91712355		104	9.35	2.09	92		0.172876
20170313T043758	0.910571	15.47803		67.16635	86.802224	1.62547	2.1580173		78.5	5.45	2.02	106		0.138017
20170406T043759	0.849394	17.78919		90.69869	121.95122	1.853485	2.40883369		61	8.8	2.135	90.5		0.273834
20170418T043759	0.789169	18.64423		94.28915	125	1.684169	2.22258622		63	7.45	1.74	75		0.482586
20170512T043800	0.830928	13.55441		90.57873	101.0101	1.377407	1.88514715		80.5	8.1	1.875	68		0.010147
20170524T043801	0.853679	18.25362		92.89127	101.0101	1.503698	2.02406753		70	8.5	2.57	63.5		0.545932
20170605T043802	0.864833	18.55678		92.75911	120.48193	1.787317	2.33604877		45.5	8.15	1.925	88		0.411049
20170629T043803	0.890337	7.050044		95.90614	114.94253	1.679457	2.21740304		75	8.15	2.295	81		0.077597
20170711T043804	0.773549	19.75932		90.52086	90.909091	1.132853	1.61613832		59.5	6.65	1.675	79.5		0.058862
20170723T043804	0.901249	24.13868		92.60256	151.51515	1.800684	2.35075191		75	5.7	2.395	82.5		0.044248
20170816T043806	0.829031	22.96289		96.07634	107.52688	1.235696	1.72926515		79	7.65	2.1	95		0.370735
20170921T043807	0.913726	18.10003		95.71059	125	2.008616	2.57947787		60	8.1	2.19	71		0.389478
20171015T043808	0.829466	14.45828		94.03771	117.64706	1.60145	2.13159496		68	8.5	2.09	79		0.041595
20171202T043807	0.899607	21.83215		90.74406	129.87013	1.703396	2.24373528		65	8.8	2.76	350		0.516265
20171226T043806	0.8544	27.07289		93.62148	126.58228	1.271597	1.76875719		102	7.2	1.93	61		0.161243
20170424T043717	0.855724	15.24808		93.99091	116.27907	2.077163	2.65487881		72	10	2.41	98		0.244879
20170506T043718	0.842172	15.65585		92.33731	102.04082	1.747222	2.29194444		69	8.7	2.36	85		0.068056
20170518T043719	0.895909	24.53152		96.05419	151.51515	1.76135	2.30748478		81	9.4	2.72	80		0.412515
20170705T043721	0.8964	15.20925		91.33222	116.27907	2.181453	2.76959846		65	10	2.42	84		0.349598
20170729T043723	0.85764	30.73492		92.72631	158.73016	1.409881	1.92086858		39	9	1.84	88		0.080869
20170810T043723	0.784609	14.10786		101.5601	113.63636	1.463203	1.97952327		73	8	1.65	124		0.329523
20170903T043724	0.842839	27.0111		96.66666	129.87013	1.289917	1.78890862		58	5.4	1.83	173		0.041091
20171021T043726	0.940383	7.975539		90.7639	133.33333	2.057678	2.63344608		61	8.7	3.08	66		0.446554
20171126T043725	0.904022	18.88573		91.86768	108.69565	1.656179	2.1917973		63	10.9	2.83	60		0.638203



Red : High Wind  
Blue: Low- Med Wind

All Data

NDBC 51002

MAX	0.638203
STD	0.193136
MEAN	0.256901



### **Research Objective**

1. Evaluating semi-empirical update of significant wave height ( $H_s$ ) estimation applied to Sentinel-1 SAR repository for narrow-band swell-wave spectrum on the open-ocean waters **without prior knowledge or external inputs.**
2. Evaluate the dependency between  $H_s$  and local environment (wind forcing, wave type, SAR system limitation, and imaging mechanism)

Answering our objective, our preliminary findings are as follow :

1. The surface roughness and slope variation parameters update shown consistent result  
The wavelength (m) grows longer, standard deviation (dB) grows bigger, and The slope (dB/ radians) is relatively steeper with increasing  $H_s$ . Some of the result fails this common pattern due to the high wind speed ( $> 10 \text{ ms}^{-1}$ ) or wind wave dominant sea.
2. Results show that the proposed method performs well in estimating  $H_s$  in the low to moderate wind forcing conditions (4 - 10ms<sup>-1</sup>) under any wave type in open-water areas. Lower performances are shown in strong wind conditions, and wind wave dominant environment.
3. Two dimensional median filter (with 5x5 pixels kernel size) in spatial domain and two dimensional Gaussian filter (0.0001 wavenumber/ 1km wavelength) in frequency domain are sufficient to remove outlier or noise which resulting more consistent result between varying scenes