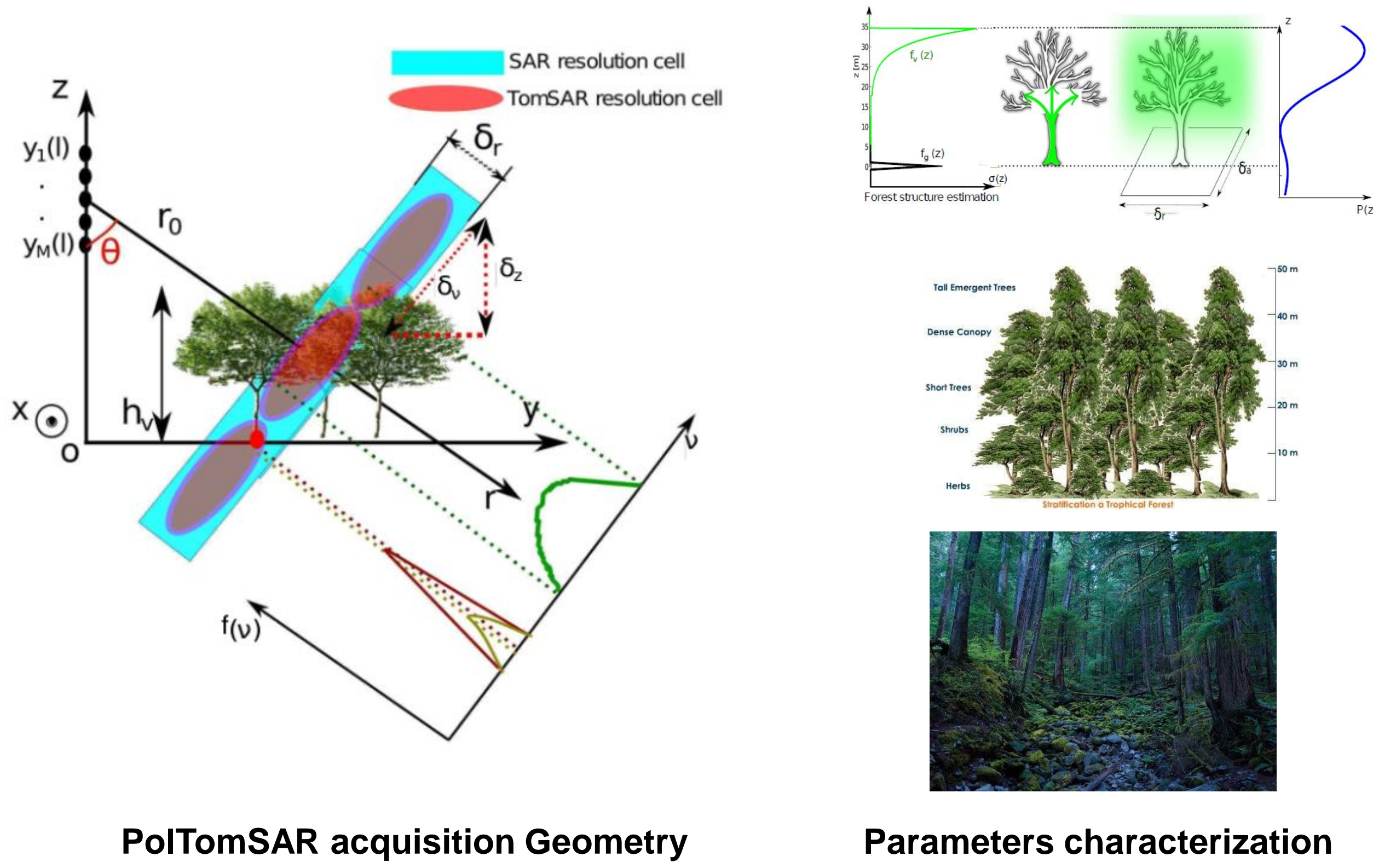


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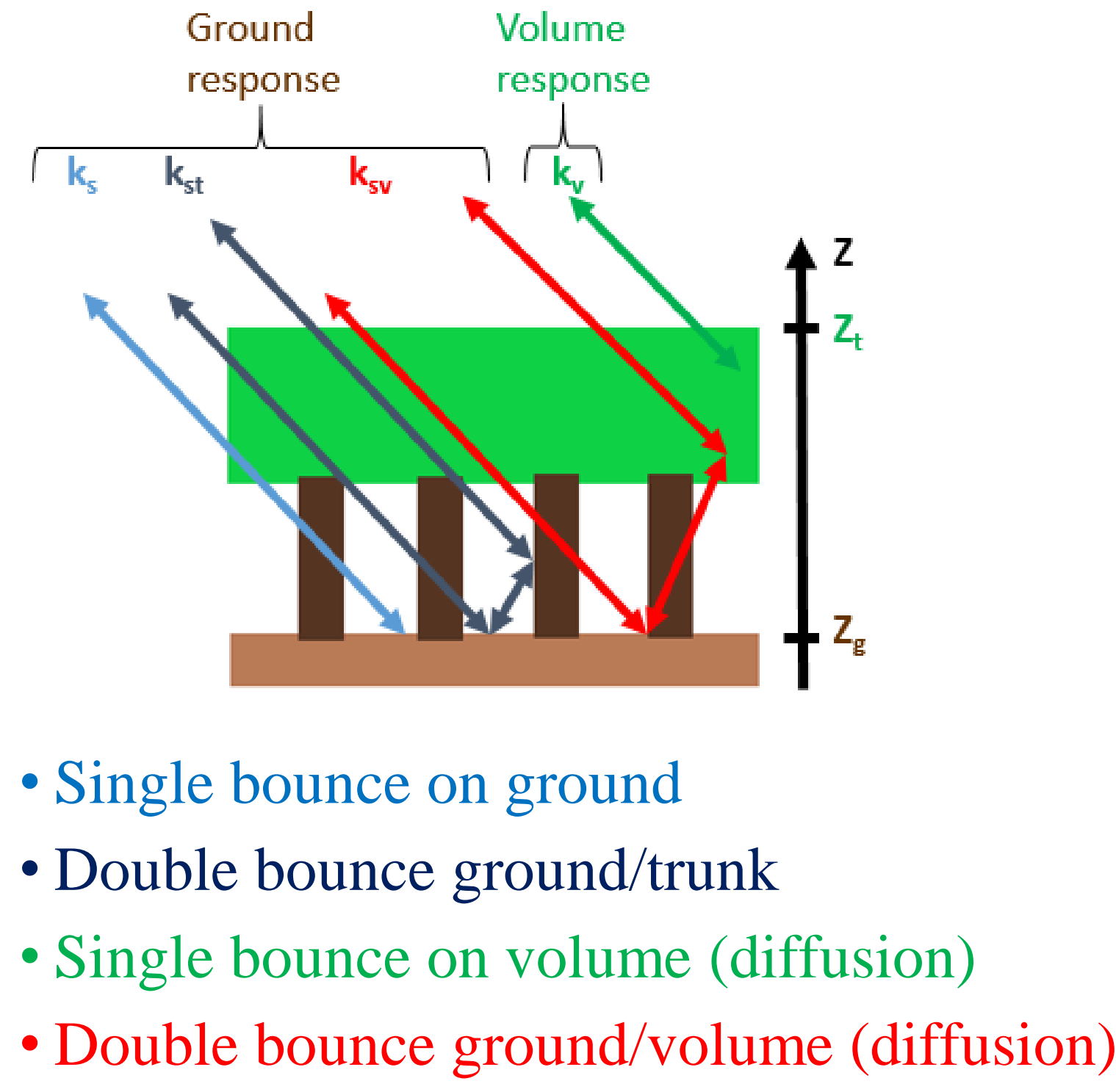
## Objectives

- Analyze coherent and incoherent double-bounce scattering mechanisms
- Separate double-bounce contributions from ground response
- Characterizing underlying ground (roughness, humidity).

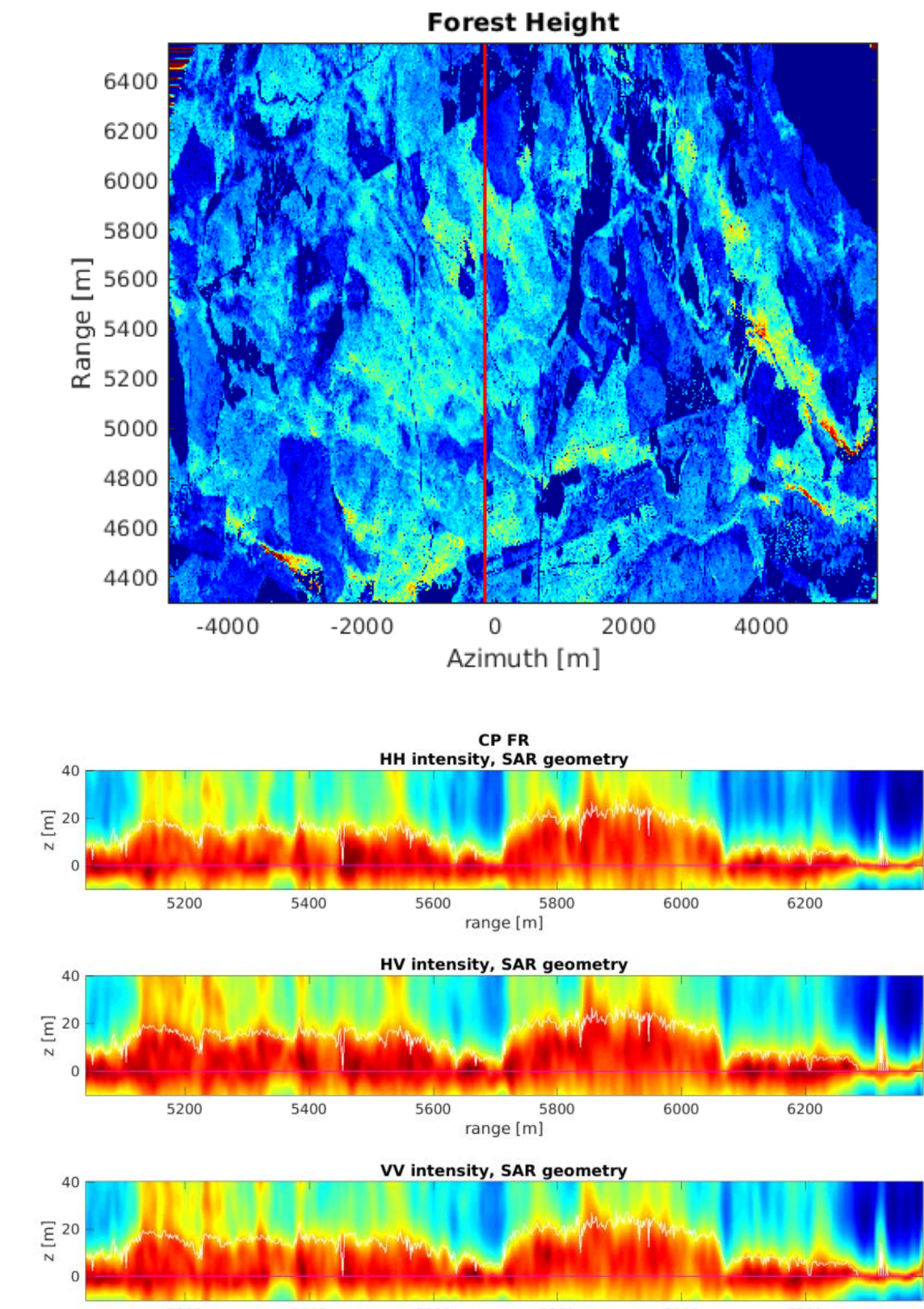
## SAR (Synthetic Aperture Radar) Tomography



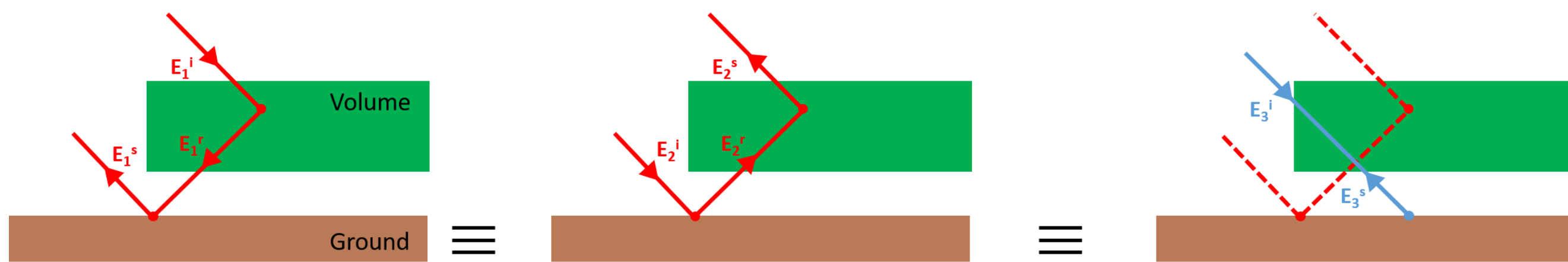
## Random Volume over Ground (RVoG) Modeling



## BioSAR II L Band



## Double-bounce scattering 2-D imaging



$$E_t^s = S_{db} E_t^i \begin{cases} \mathbf{R} = \begin{bmatrix} R_{hh} & 0 \\ 0 & R_{vv} \end{bmatrix} \\ \mathbf{S}_i = \begin{bmatrix} S_{ihh} & S_{ihv} \\ S_{ivh} & S_{ivv} \end{bmatrix} \end{cases} \quad \begin{cases} \mathbf{S}_d = \mathbf{R} \mathbf{S}_1 = \begin{bmatrix} R_{hh} S_{1hh} & R_{hh} S_{1hv} \\ R_{vv} S_{1vh} & R_{vv} S_{1vv} \end{bmatrix} \\ \mathbf{S}_u = \mathbf{S}_2 \mathbf{R} = \begin{bmatrix} S_{2hh} R_{hh} & S_{2hv} R_{vv} \\ S_{2vh} R_{hh} & S_{2vv} R_{vv} \end{bmatrix} \end{cases}$$

BSA convention

$$S_{1hh} = S_{2hh}; S_{1vv} = S_{2vv};$$

$$S_{1hv} = S_{2vh}; S_{1vh} = S_{2hv}$$

FSA convention

$$S_{1hh} = S_{2hh}; S_{1vv} = S_{2vv};$$

$$S_{1hv} = -S_{2vh}; S_{1vh} = -S_{2hv}$$

$$\mathbf{S}_{db} = \mathbf{S}_d + \mathbf{S}_u \longrightarrow \mathbf{S}_{db} = \begin{bmatrix} 2R_{hh}S_{hh} & R_{hh}S_{hv} - R_{vv}S_{hv} \\ R_{vv}S_{hv} - R_{hh}S_{hv} & 2R_{vv}S_{vv} \end{bmatrix}$$

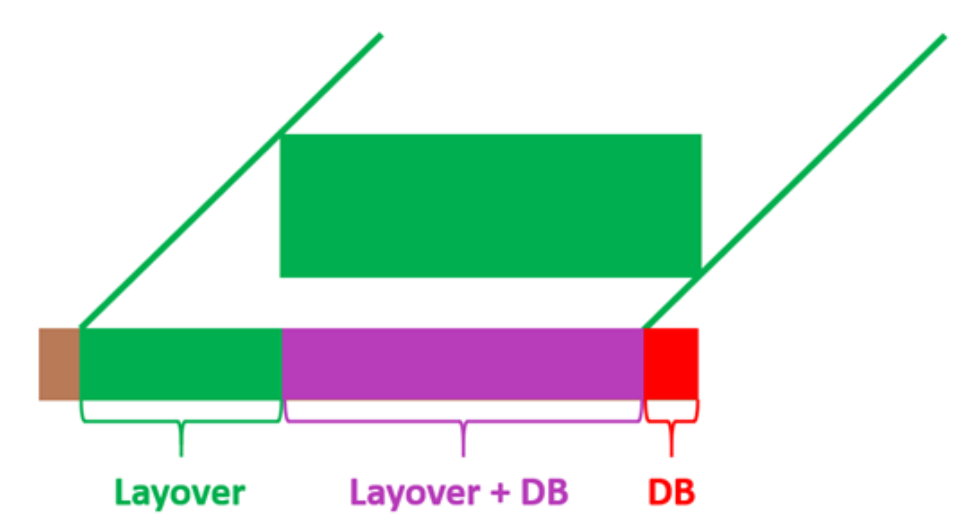
**Assumption:** The scene contains vegetation i.e. not homogeneous and speckle noise is present

**Outcome:**  $\mathbf{R}$  and  $\mathbf{S}$  are Gaussian, centered, independent scattering mechanisms  $\longrightarrow$  Intercorrelations null

Covariance matrix as a function of  $4I_{R_{hh}}$ ,  $I_{S_{hh}}$  and  $\alpha_{ipq} = \sqrt{\frac{I_{ipq}}{I_{ihh}}}$

$$\mathbf{C}_{db} = 4I_{R_{hh}} I_{S_{hh}} \begin{bmatrix} 1 & \frac{1}{2}\alpha_{Shv}\rho_{Shhvv}(1 - \alpha_{Rvv}\rho_{Rhhvv}) & \alpha_{Rvv}\rho_{Rhhvv}\alpha_{Svv}\rho_{Shhvv} \\ \frac{1}{4}\alpha_{Shv}^2(1 + \alpha_{Rvv}^2 + 2Re(\alpha_{Rvv}\rho_{Rhhvv})) & \frac{1}{2}\alpha_{Shv}\alpha_{Svv}\rho_{Shhvv}\alpha_{Rvv}(\rho_{Rhhvv} - \alpha_{Rvv}) \\ \alpha_{Rvv}^2\alpha_{Svv}^2 \end{bmatrix}$$

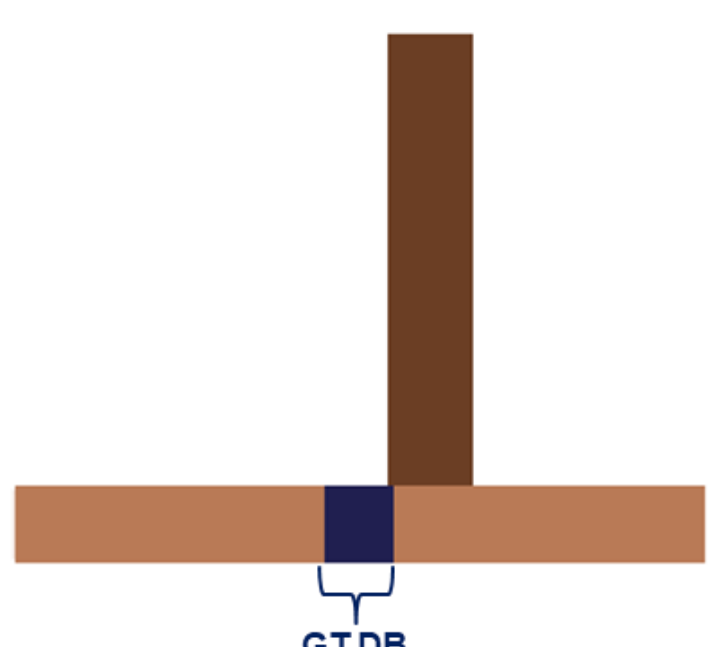
Ground/Volume scattering  $\gamma \approx 0$



$$\mathbf{C}_{gv} = 4I_{R_{hh}} I_{S_{hh}} \mathbf{P}_{gv} \begin{bmatrix} 1 & 0 & \gamma \approx 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix} \mathbf{P}_{gv}$$

- Incoherent double-bounce
- Focused on the ground below the volume
- Occurs over the majority of the scene

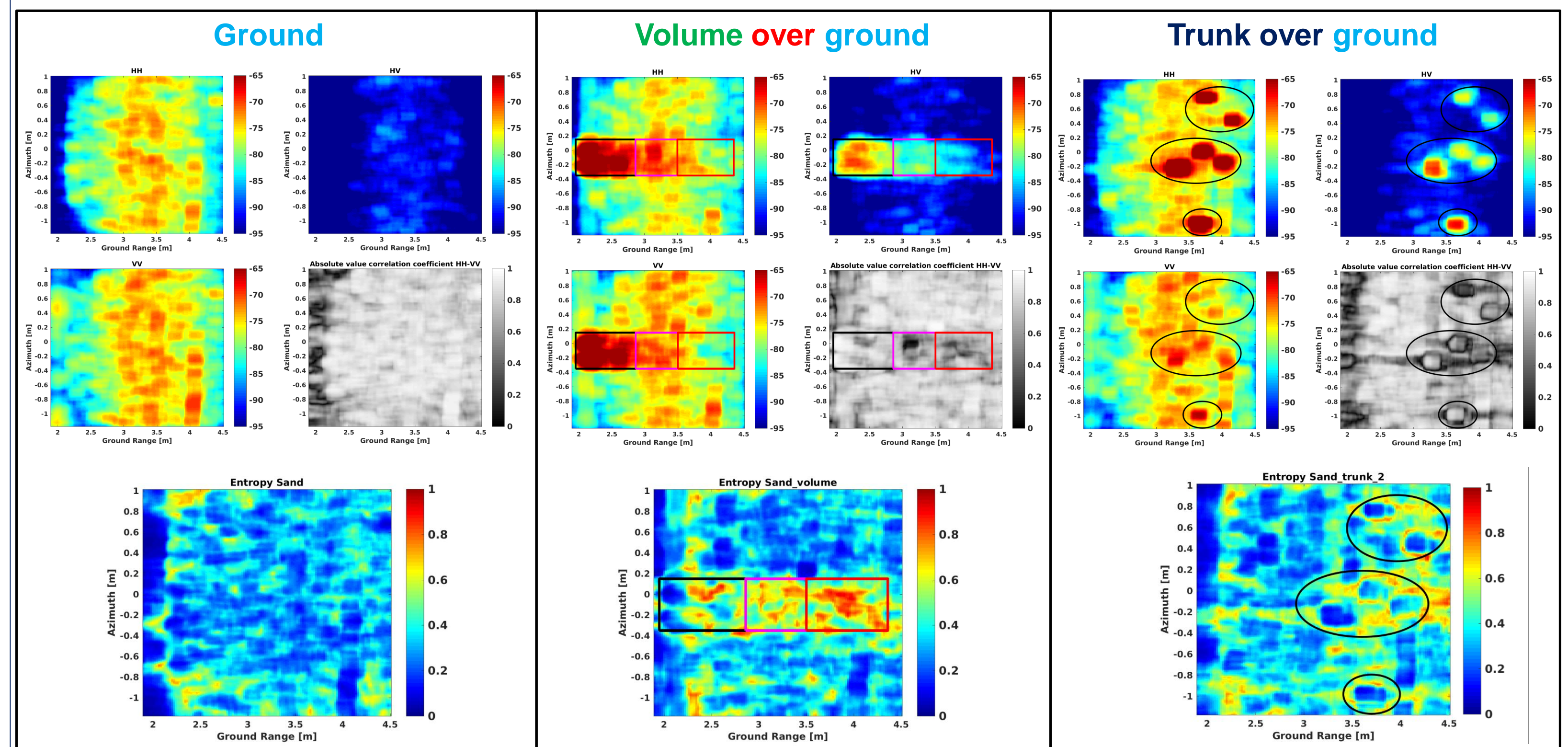
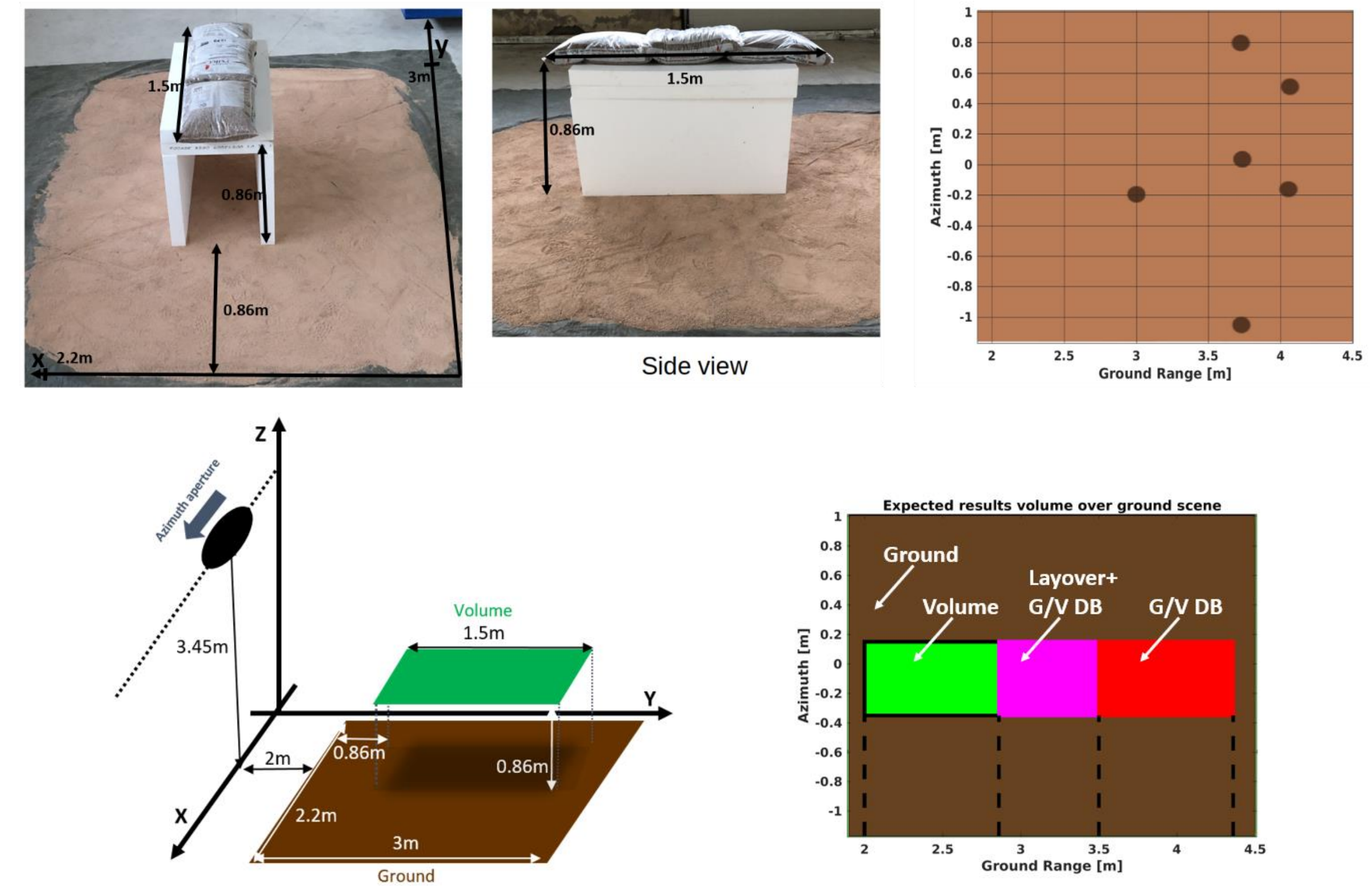
Ground/Trunk scattering  $\gamma \approx 1$



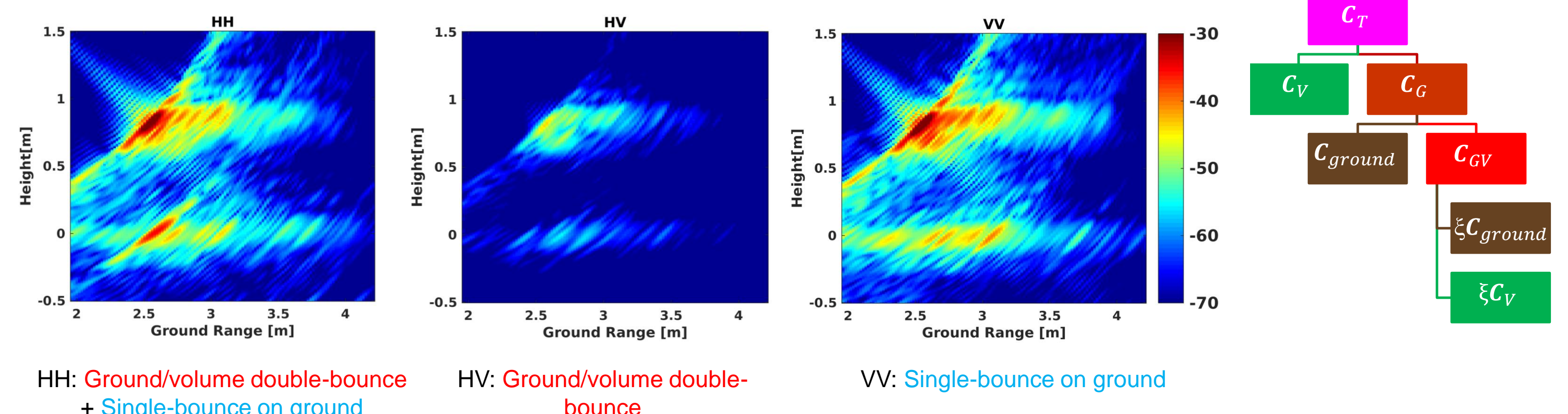
$$\mathbf{C}_{gt} = 4I_{R_{hh}} I_{S_{hh}} \mathbf{P}_{gt} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix} \mathbf{P}_{gt}$$

- Coherent double-bounce
- Focused on the ground at the bottom of the trunk
- Occurs over a very small part of the scene

## Geometry acquisition & PolSAR results



## PolTomSAR results and proposed solution



## Conclusion:

Double-bounce GT is coherent meaning that its contributions can be avoided.

Double-bounce GV is incoherent and cannot be avoided.

Pure ground contributions are retrieved by subtracting a portion of volume contributions.