



# Estimation of Tropospheric Delays in Multi-Temporal InSAR

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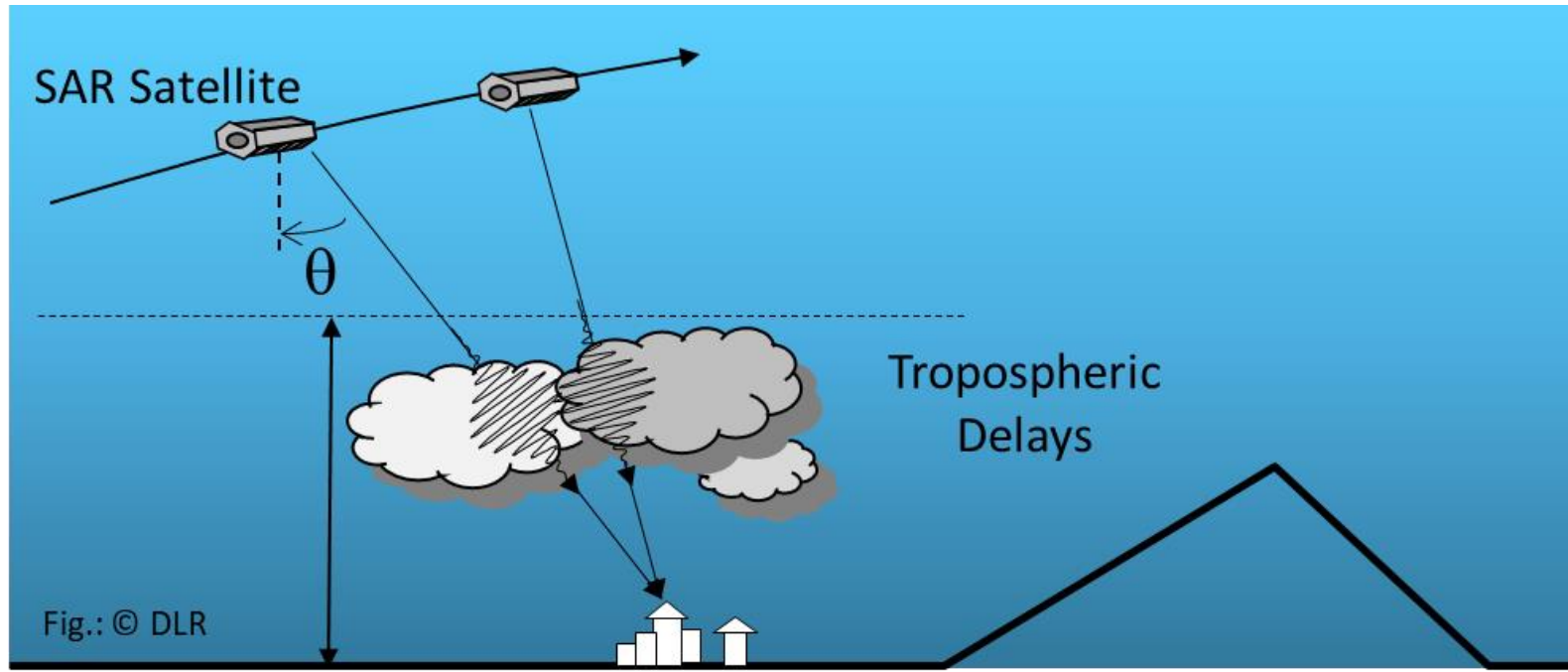
2019 年6月 24-28 日 斯洛文尼亚 卢布尔雅那



# OUTLINE

1. Introduction
2. Methodology
3. Experiments
4. Conclusions





## Characteristics:

- Related to temperature, pressure, humidity, etc.
- Varying in space and time



## Based on auxiliary data:

- GNSS
- Radiometric measurements
- Weather model

Limitations:

- Low spatial/temporal resolutions
- Limited overall accuracy

## Based on InSAR data

- Stacking, spatiotemporal filter
- Correction based on elevation

Limitations:

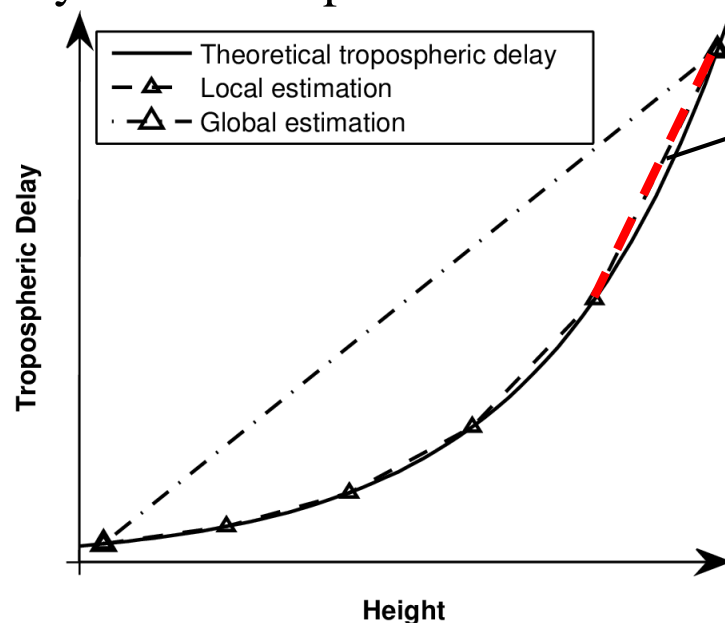
- Accuracy often limited

Limitations:

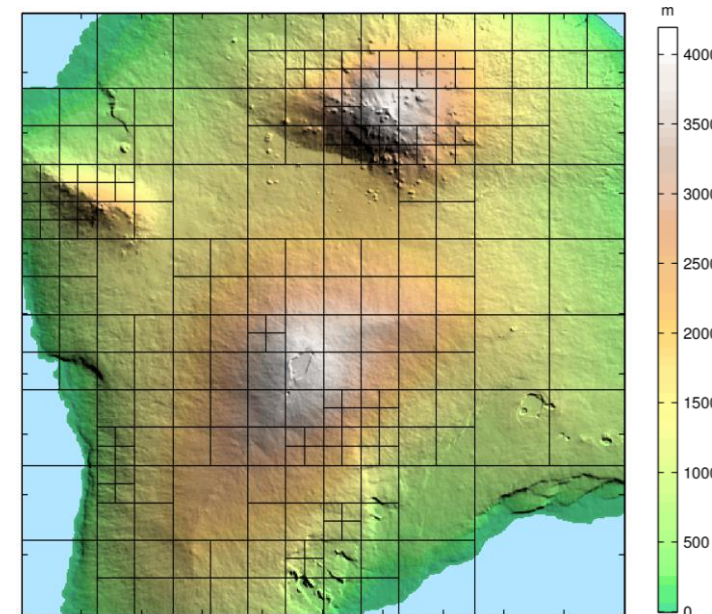
- Spatial variability
- Effects of other signals (e.g. deformation, topographic error)

$$\phi_{trop} = K \cdot \Delta h + \phi_0$$

- Divide an area of study into overlapping windows
- Window size varies with slope gradient as aided by a quadtree model
- Assume linear phase-elevation model within each window
- Estimate tropospheric delays jointly with other parameters



Linear phase-elevation  
model in local area



$$\phi_{trop} = K \cdot \Delta h + \phi_0$$

Jointly estimate TD, deformation and topographic errors

- Tropospheric delay difference:

$$\Delta\phi_{tropo,slc,p,q}^i = (h_p - h_q) \cdot K_{slc}^i$$

$h_p, h_q$ : elevations for point  $p$  and  $q$

$K_{slc}^i$ : tropospheric delay coefficient for single SAR image

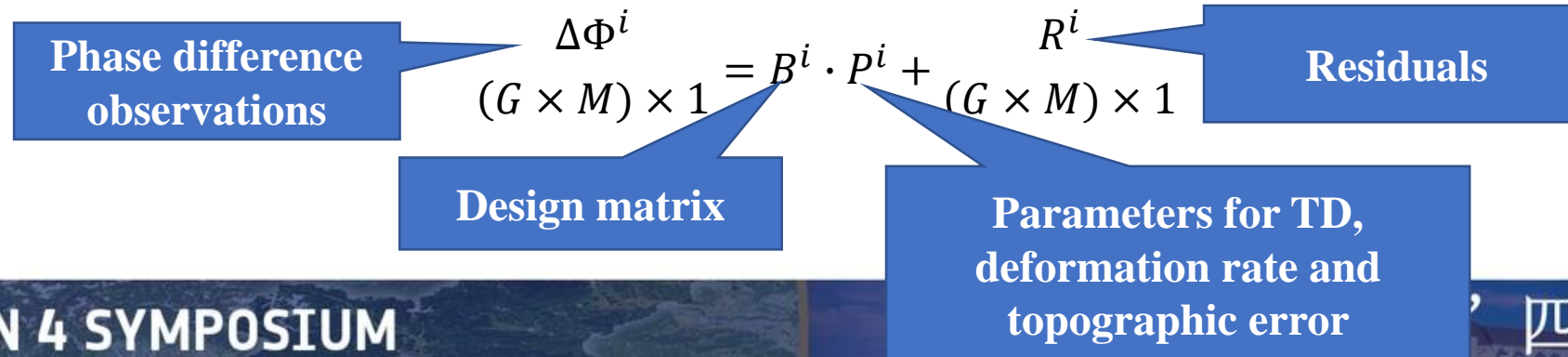
- Deformation rate & topographic error:

$$\phi_{defo+topo,p}^i = \begin{bmatrix} -\frac{4\pi}{\lambda} \cdot T_j & -\frac{4\pi}{\lambda} \cdot \frac{B_{\perp,j}}{r \cdot \sin\theta} \end{bmatrix} \cdot \begin{bmatrix} v_p \\ \Delta h_p \end{bmatrix}$$

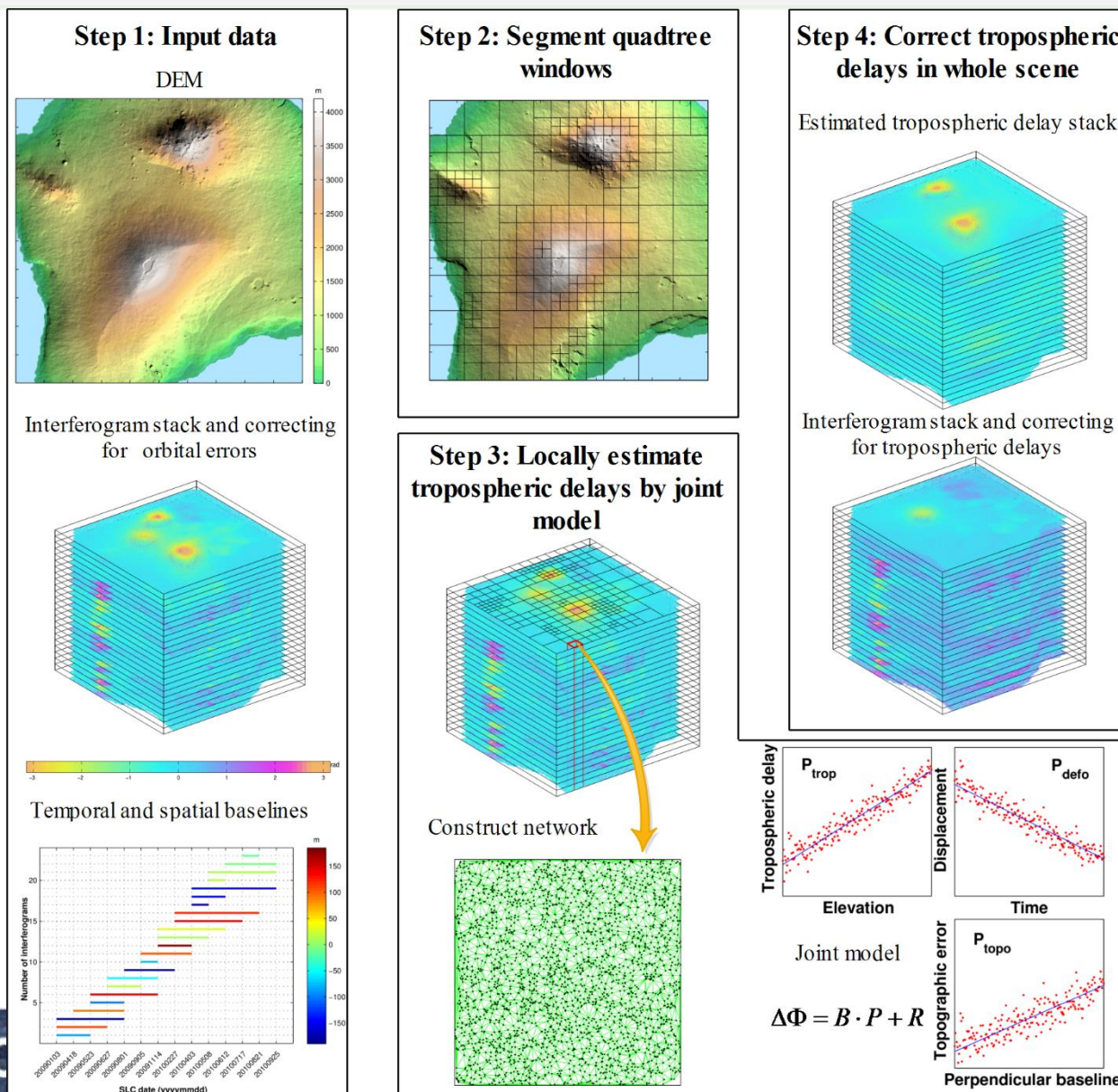
$v_p, \Delta h_p$ : deformation rate and topographic error for point  $p$

$T_j, B_{\perp,j}$ : temporal and spatial baseline

- Joint model construction

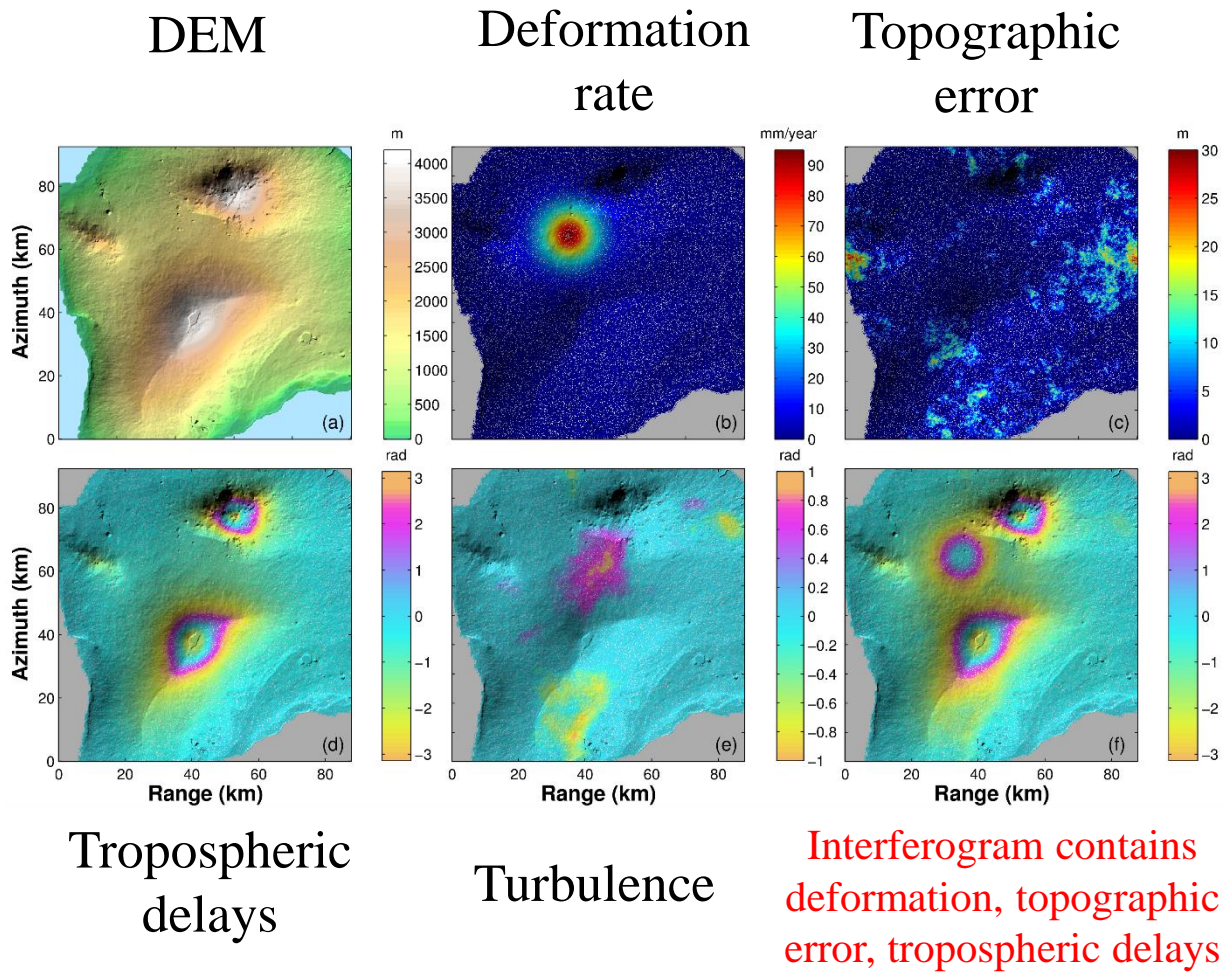








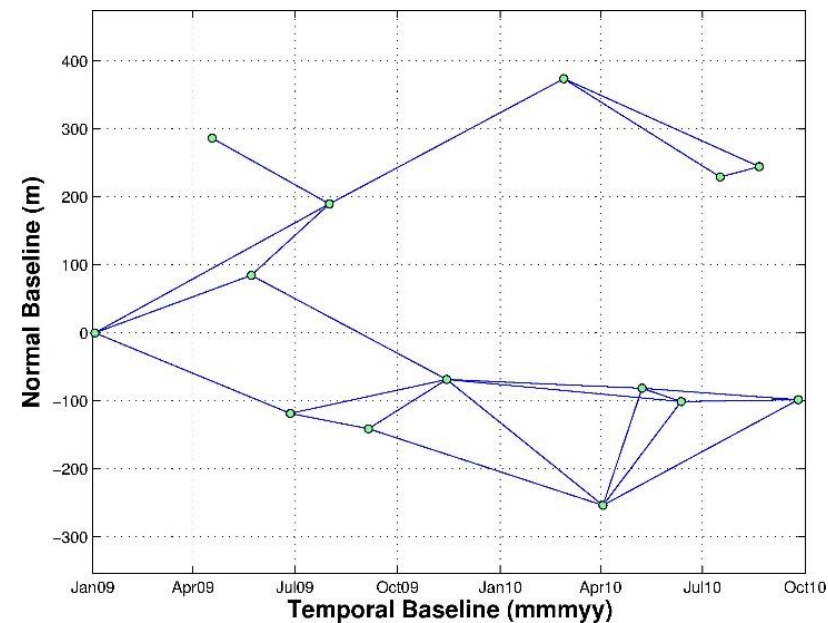
## Signal components:



## Baselines:

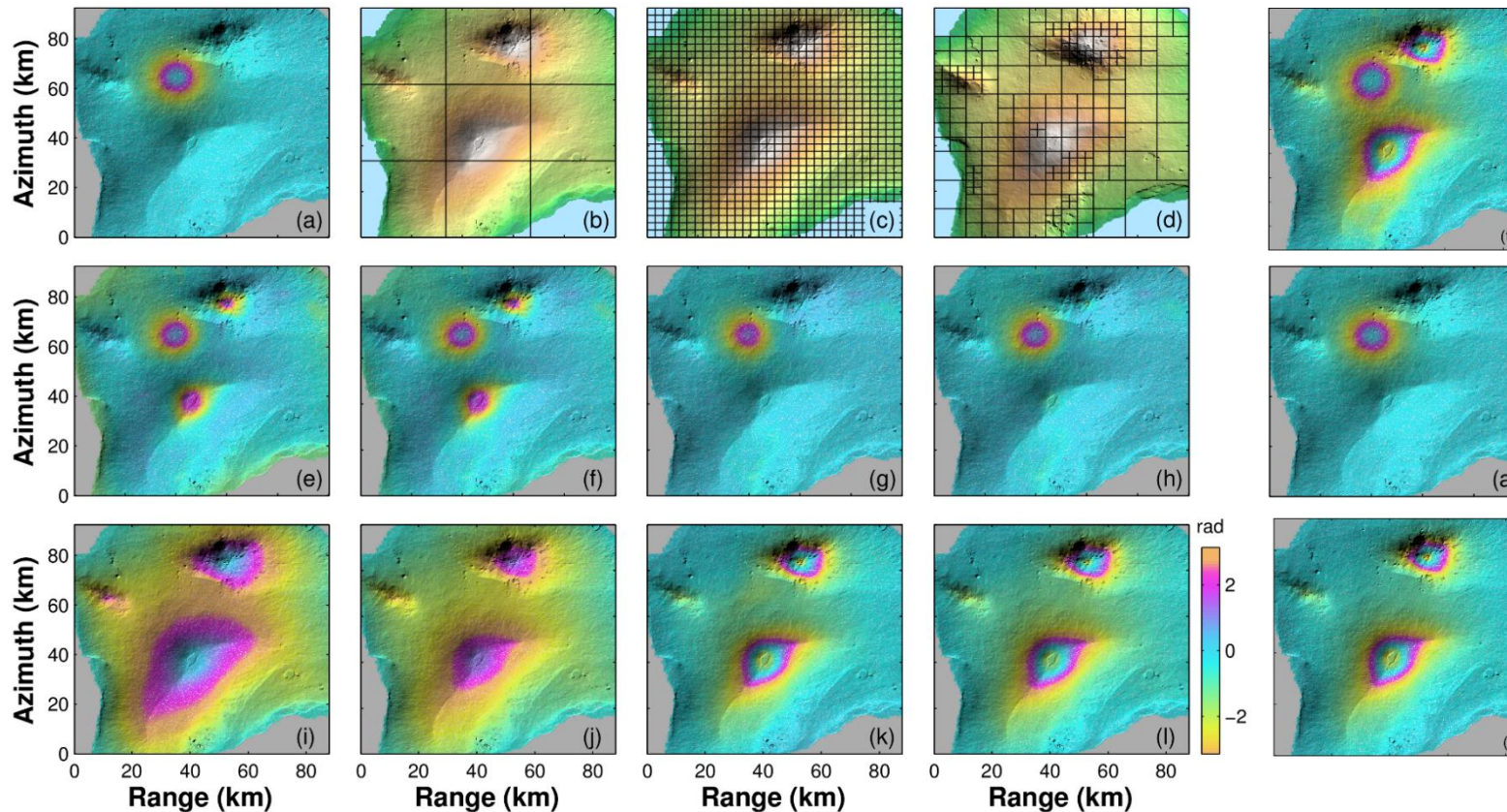
14 SAR images

23 interferograms





Global linear      3x3 regular window      32x32 regular window      Quadtree joint model



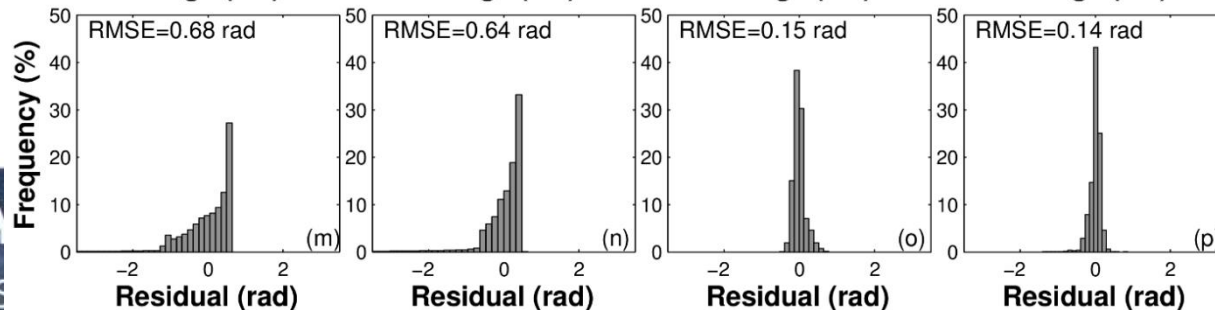
Interferogram  
before correction

Corrected  
interferogram

Estimated  
tropospheric  
delays

True values

TD difference  
between estimation  
and simulation

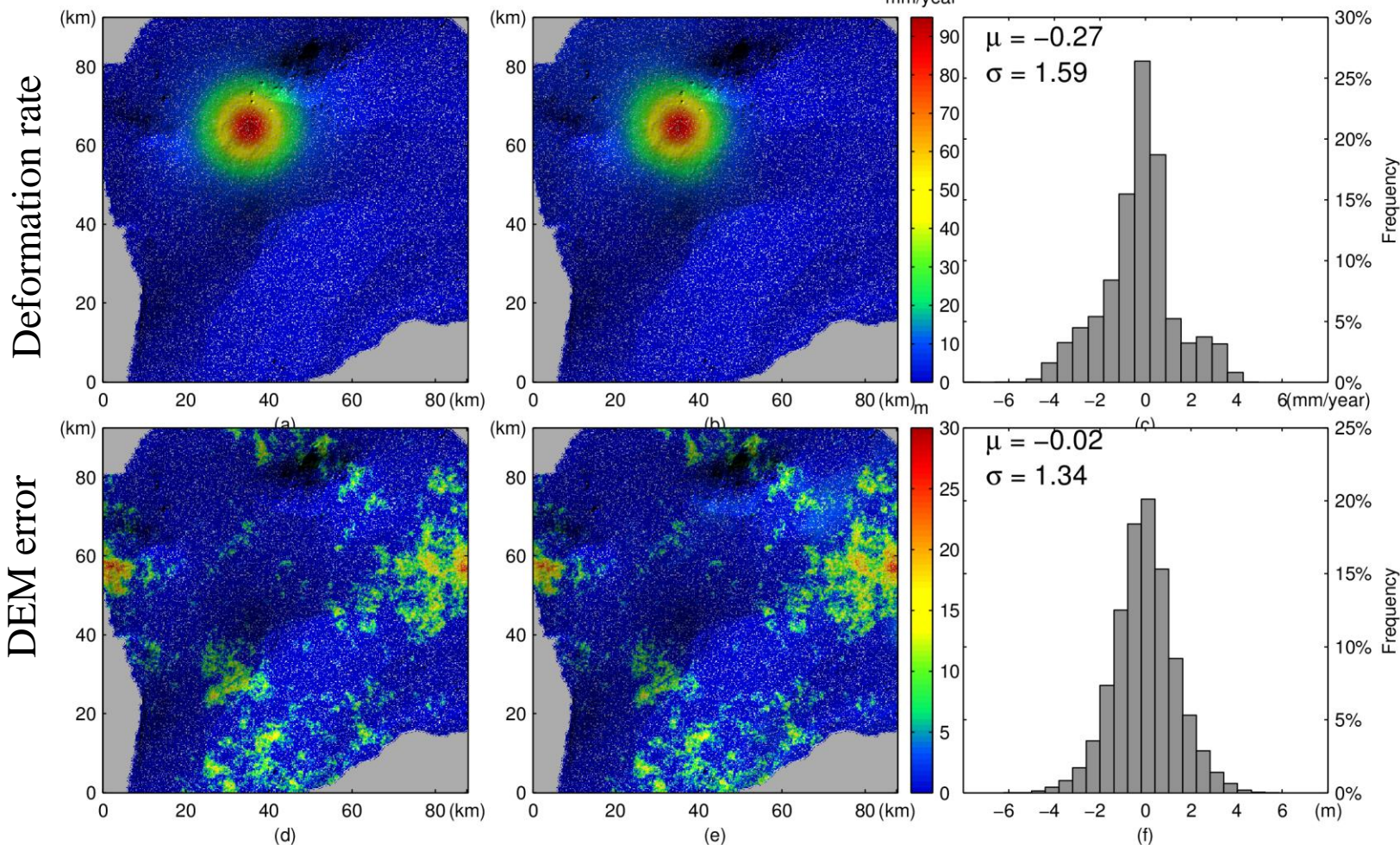




Simulation

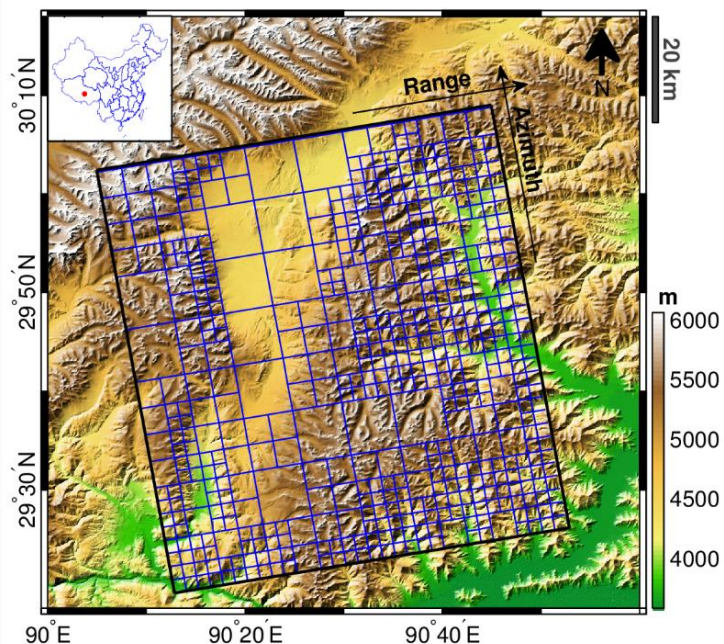
Estimation from  
quadtree joint model

Difference between  
estimation and simulation



	Standard deviation of estimation error	
	Deformation rate (mm/year)	DEM error (m)
Global linear method	1.74	1.42
3x3 regular window	1.71	1.41
32x32 regular window	2.13	1.33
Quadtree joint model	1.59	1.34





**Location:** Dangxiong, Tibet, China

**Data:** ALOS/PALSAR-1

**Period:** Dec 2006 – Jul 2008

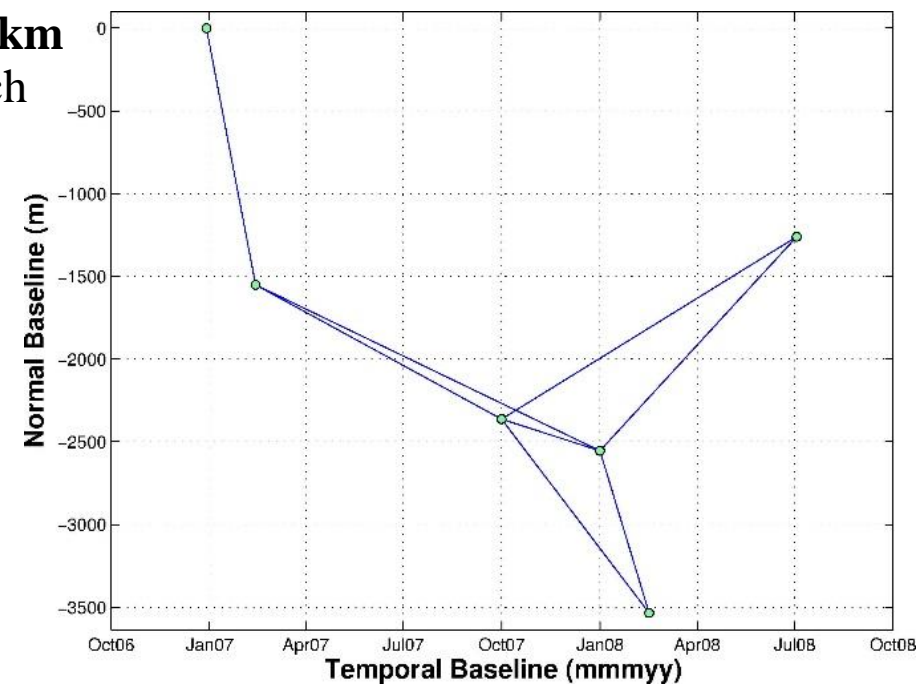
Pre-seismic deformation

Number of windows: **526**

Size of smallest window: **2km x 2km**

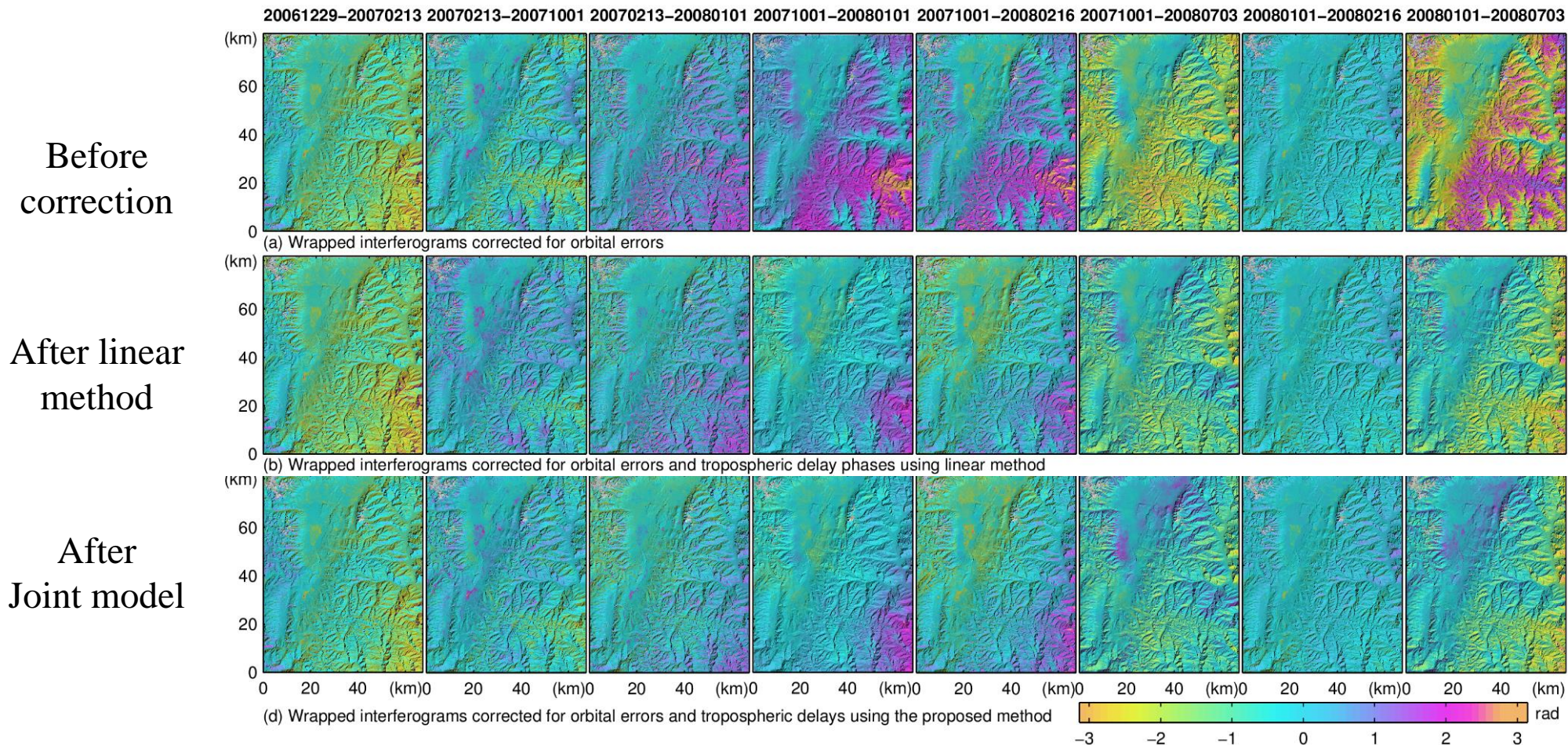
Maximum height difference in each window: **1km**

Interferometric pair	Perpendicular baseline (m)	Temporal baseline (day)
20061229-20070213	1552	46
20070213-20071007	813	230
20071001-20080101	192	92
20071001-20080216	1174	138
20071001-20080703	-1105	276
20080101-20080216	981	46
20080101-20080703	-1297	184



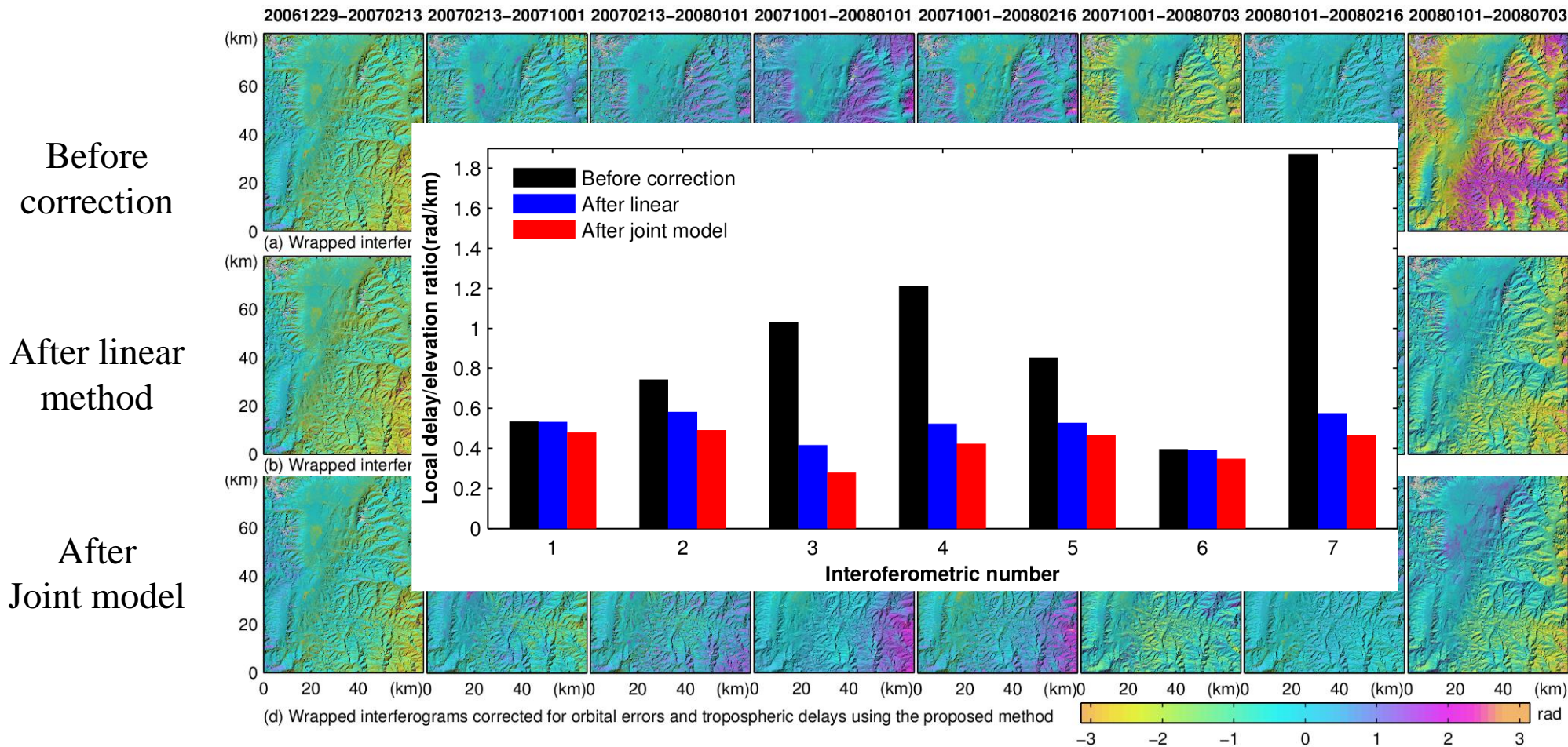


## Effects of corrections on interferograms





## Statistical analysis: Relationships between unwrapped phase and elevation



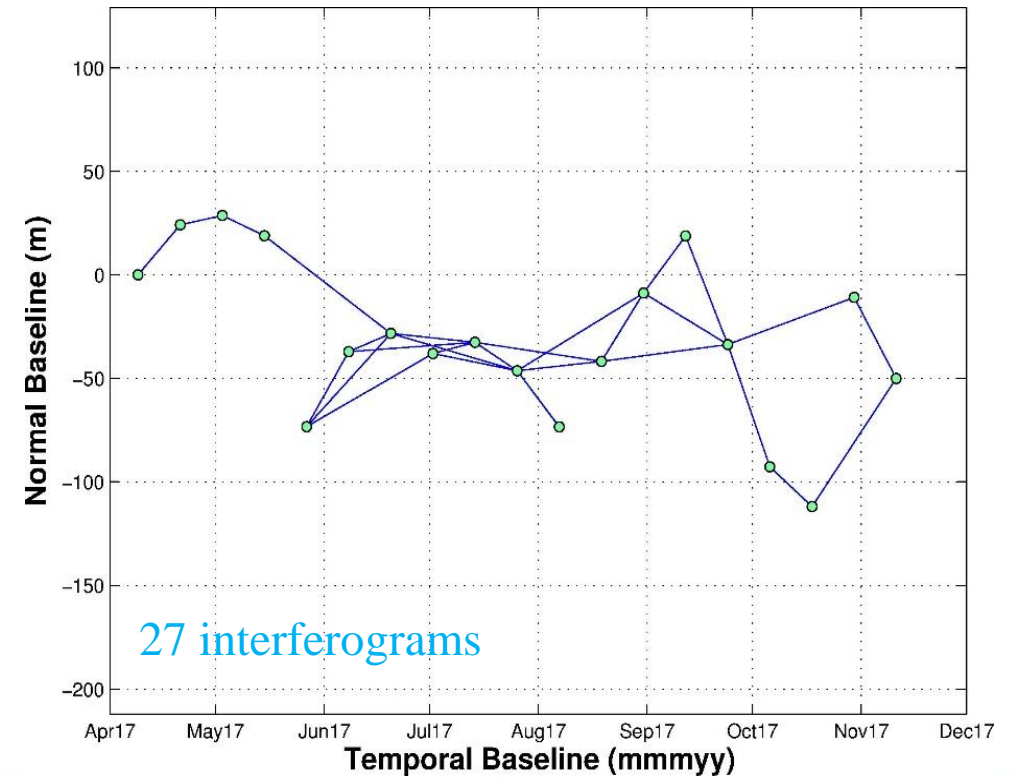
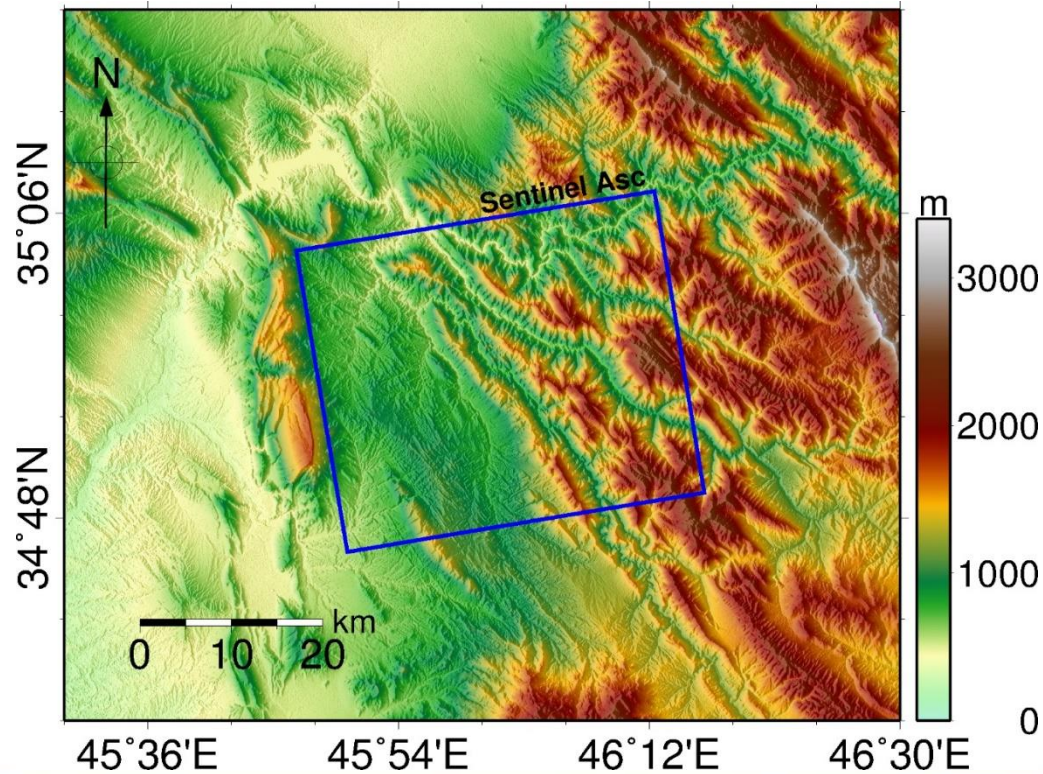


**Location:** Iran-Iraq border

**Dataset:** 19 ascending Sentinel-1A

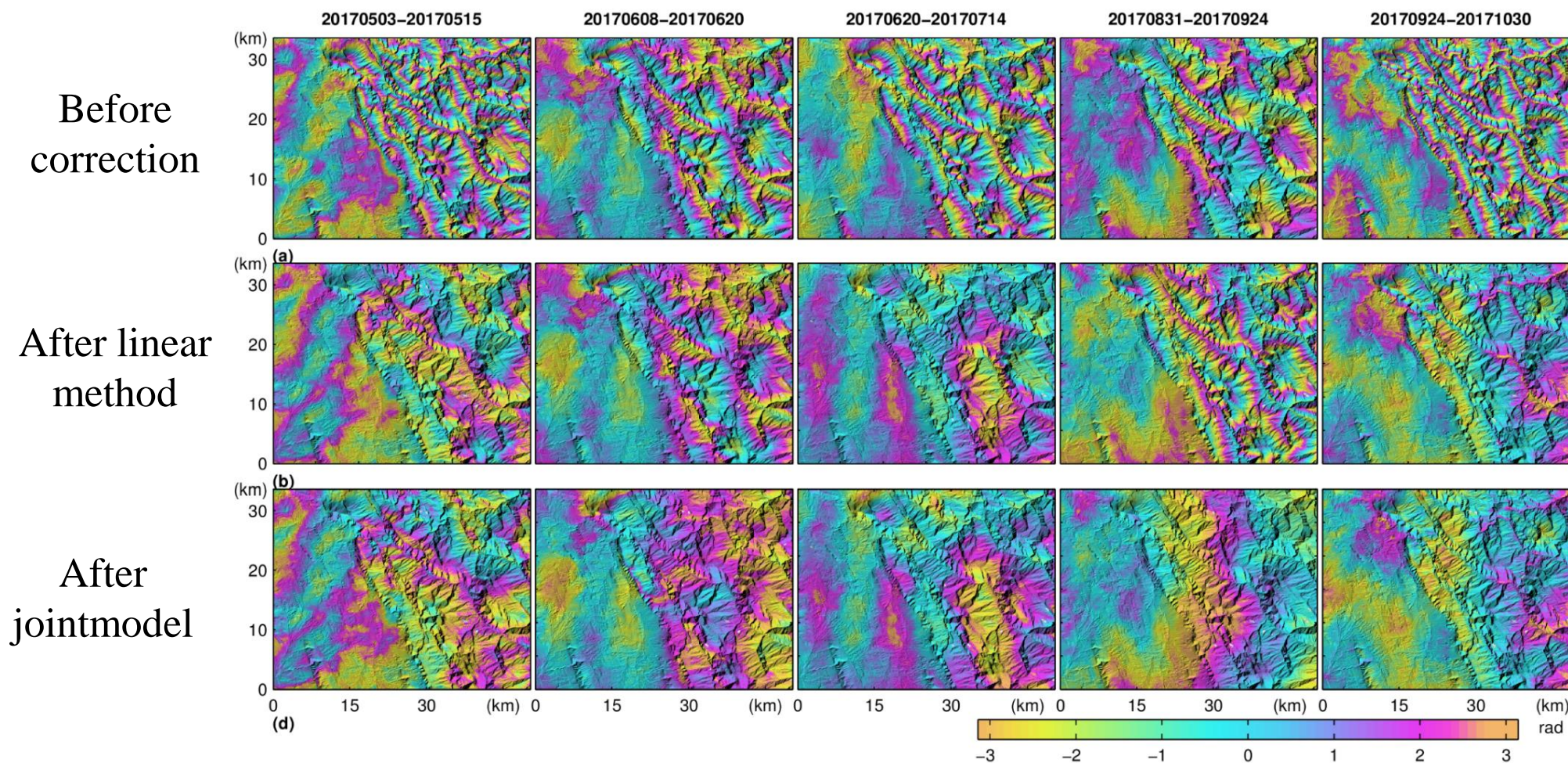
**Period:** April 2017 – November 2017

**Deformation:** Pre-seismic



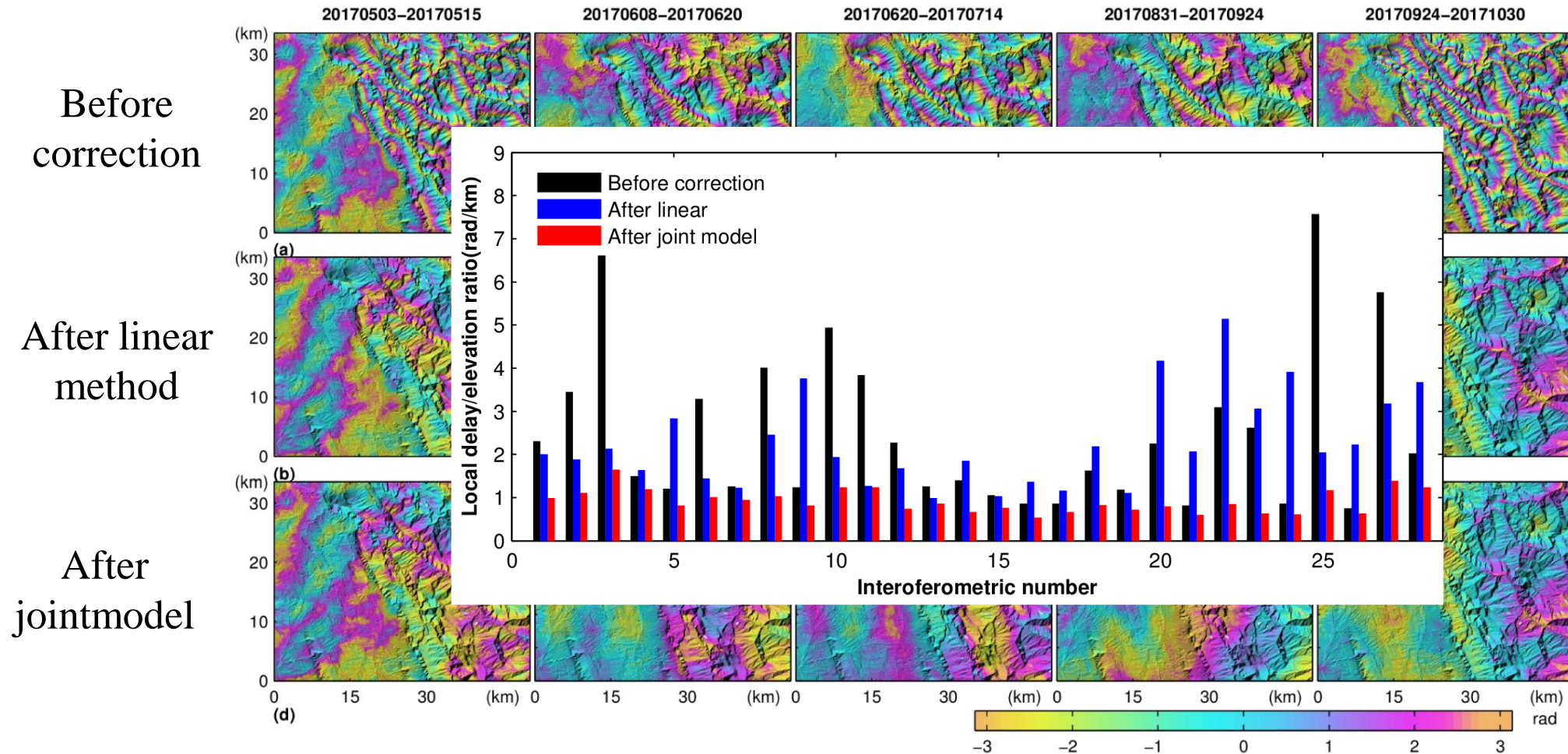


## Correction of Tropospheric Delays





## Statistical analysis: Relationships between unwrapped phase and elevation

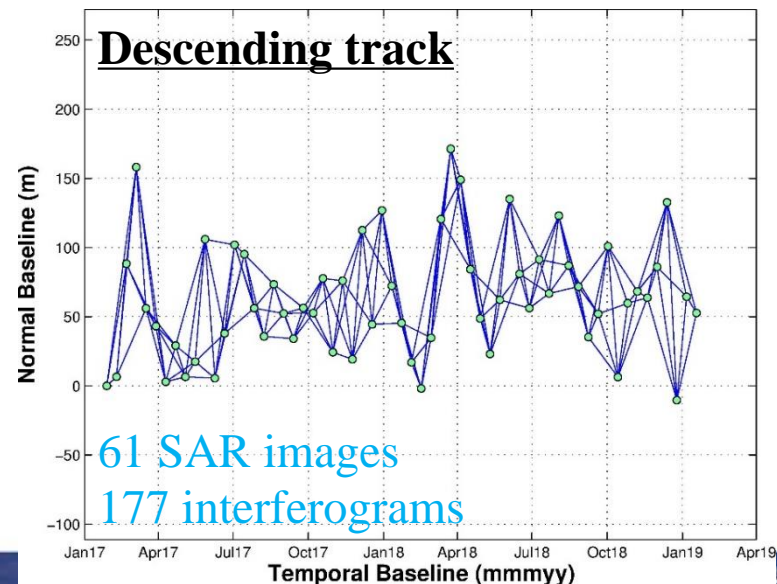
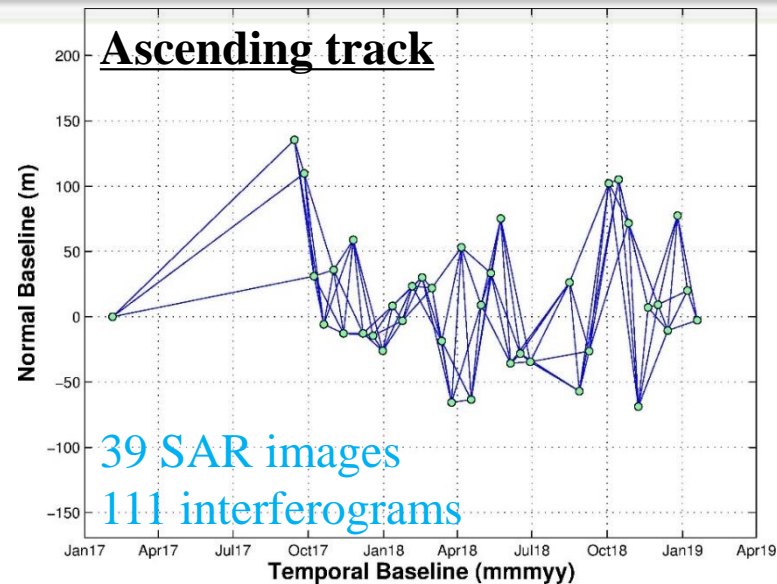
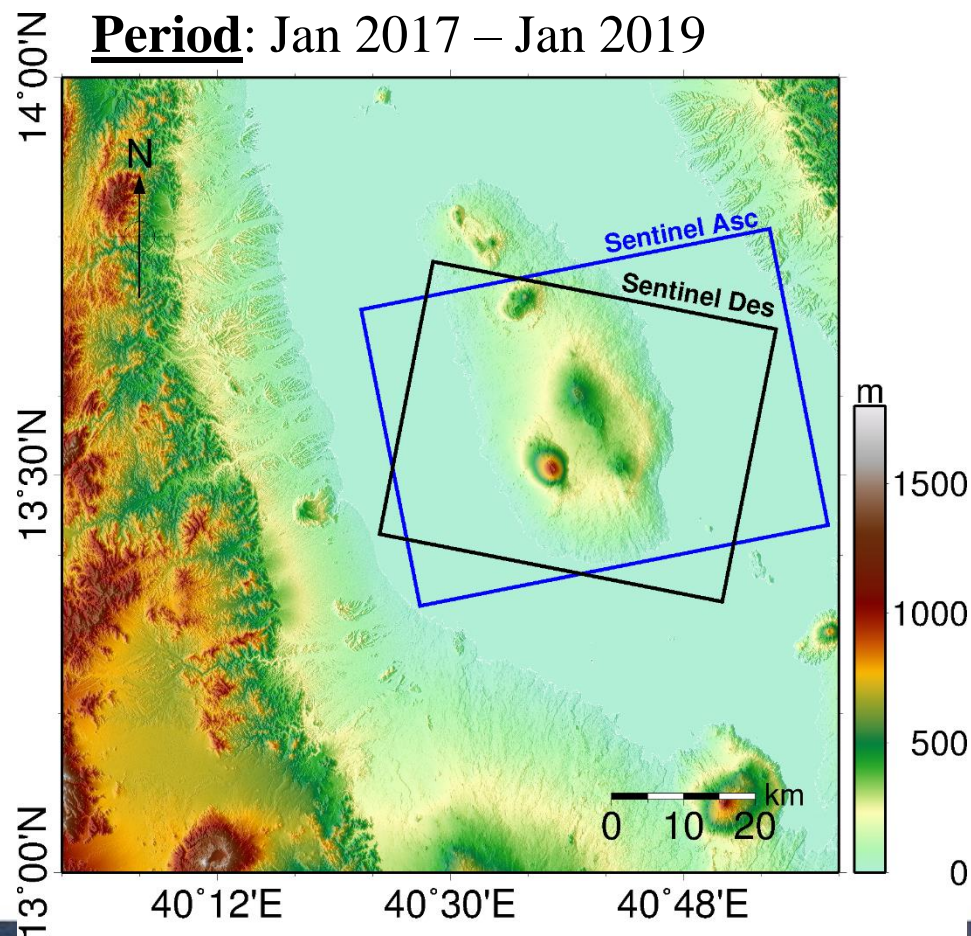




**Location:** Ale Bagu Volcano, Ethiopia

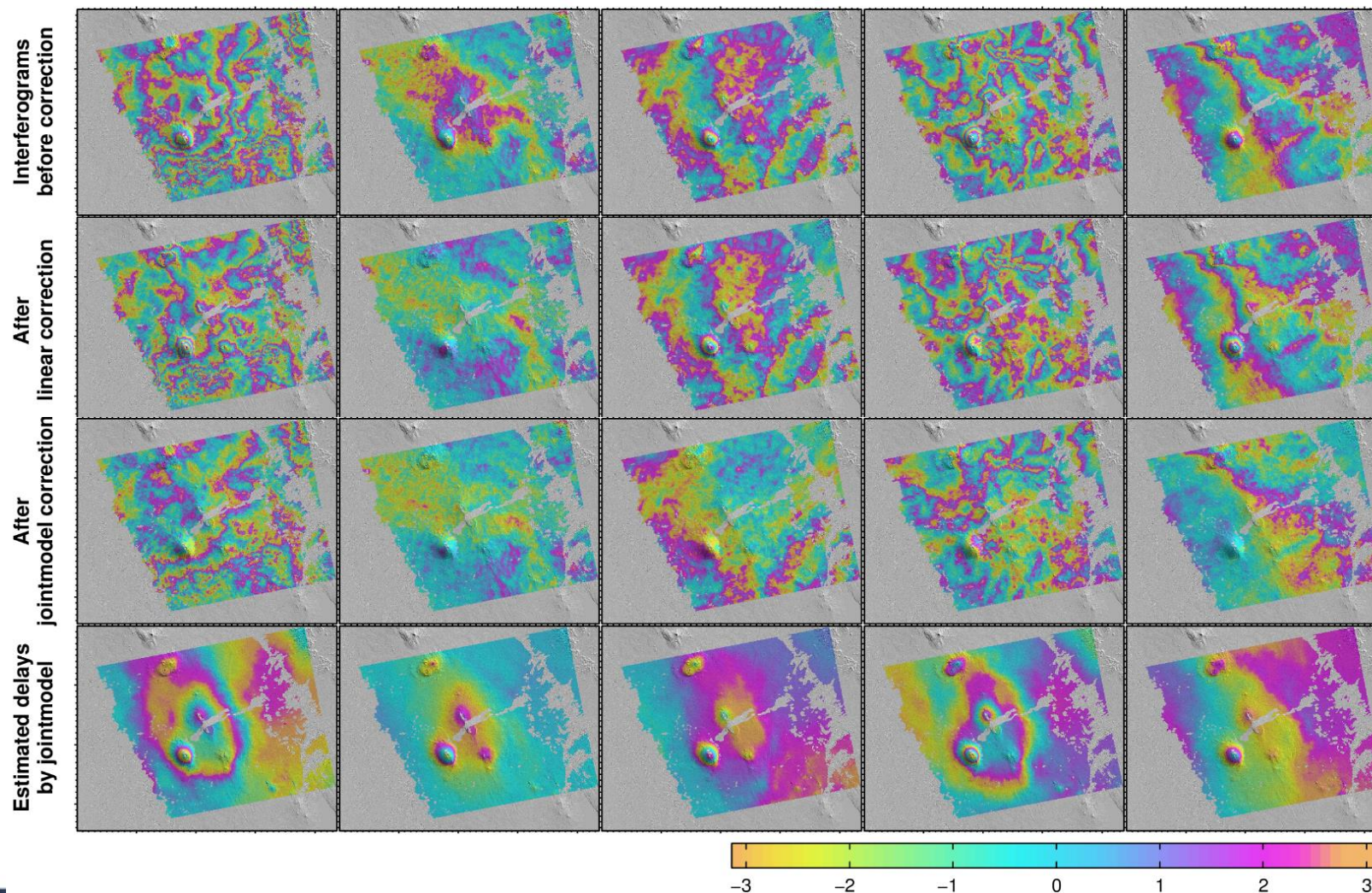
**Dataset:** 39 ascending and 61 descending Sentinel-1A

**Period:** Jan 2017 – Jan 2019



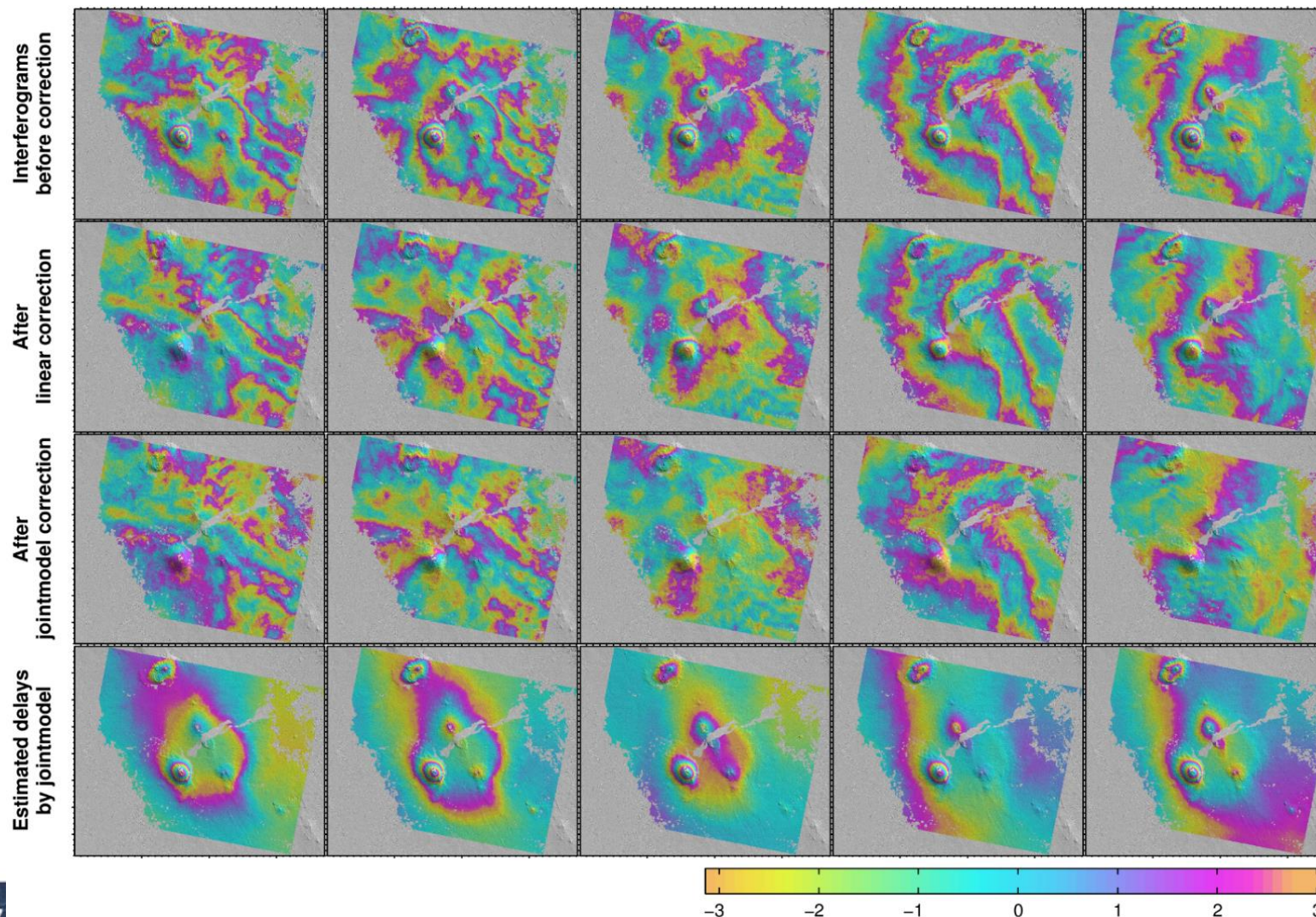


## Ascending Track – Tropospheric delay correction results





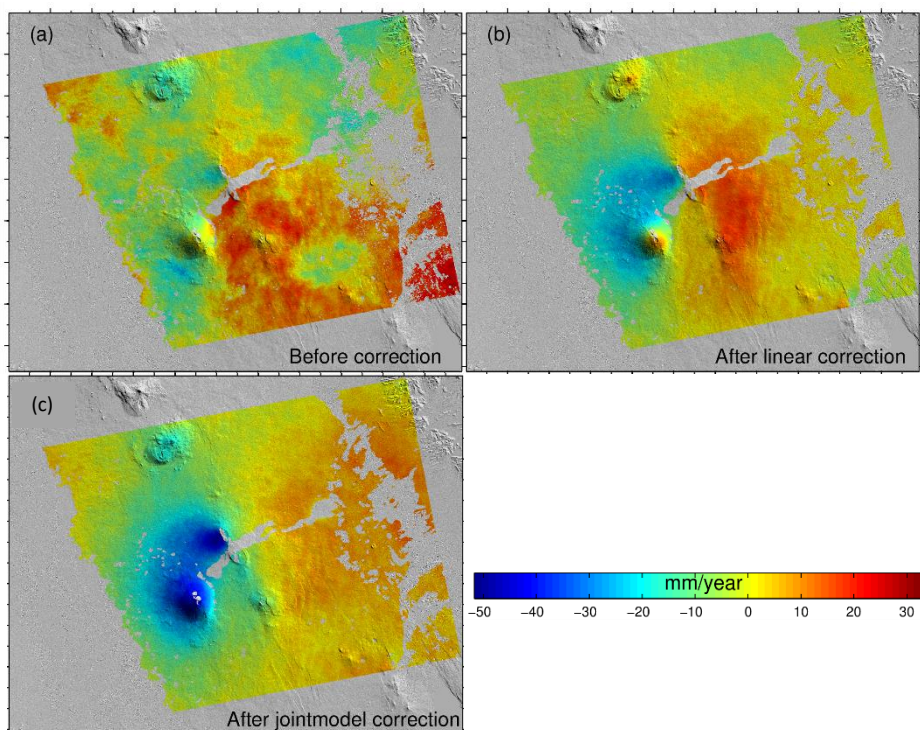
## Descending Track – Tropospheric delay correction results



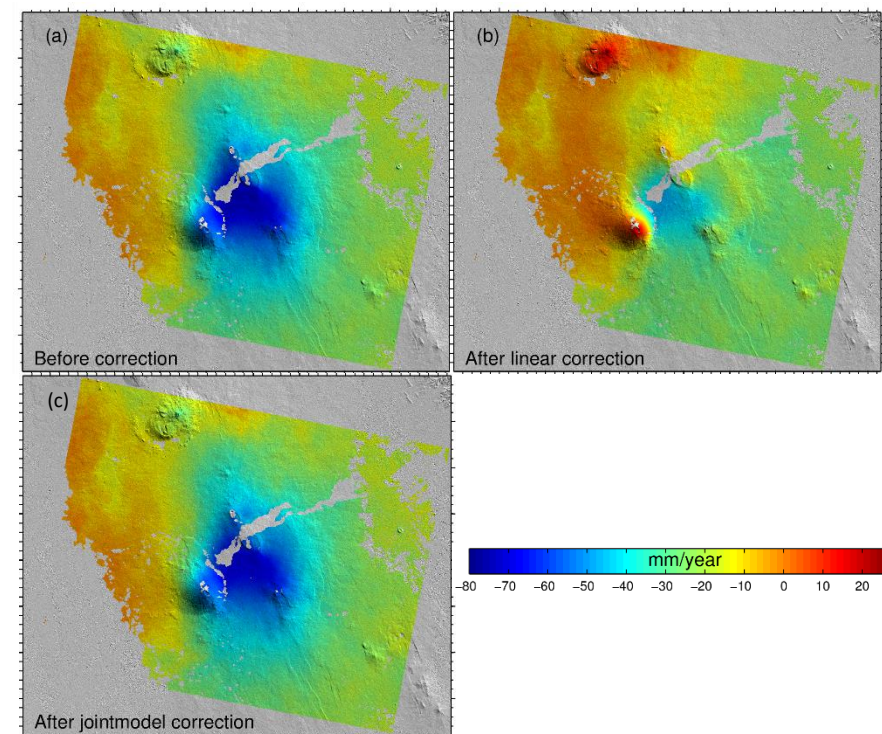


## Deformation rate maps

### Ascending Track



### Descending Track





- A new approach for joint estimation of tropospheric delays and other parameters in multi-temporal InSAR has just been proposed.
- Experimental results have demonstrated the approach is effective.

Liang, H., Zhang, L., Ding, X., Lu, Z., & Li, X. (2018). Toward Mitigating Stratified Tropospheric Delays in Multitemporal InSAR: A Quadtree Aided Joint Model. *IEEE Transactions on Geoscience and Remote Sensing*, (99), 1-13.